

Global Neutrino Oscillation Fits

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SHAPING THE GLOBAL PICTURE

A Successful Scenario

flavor eigenstates

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$
mass eigenstates

$U = V \text{diag}(1, e^{i\alpha_2/2}, e^{i\alpha_3/2})$
 Extra CP Violating phases only if Majorana

Pontecorvo-Maki-Nakagawa-Sakata Mixing Matrix

$$V = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13} e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

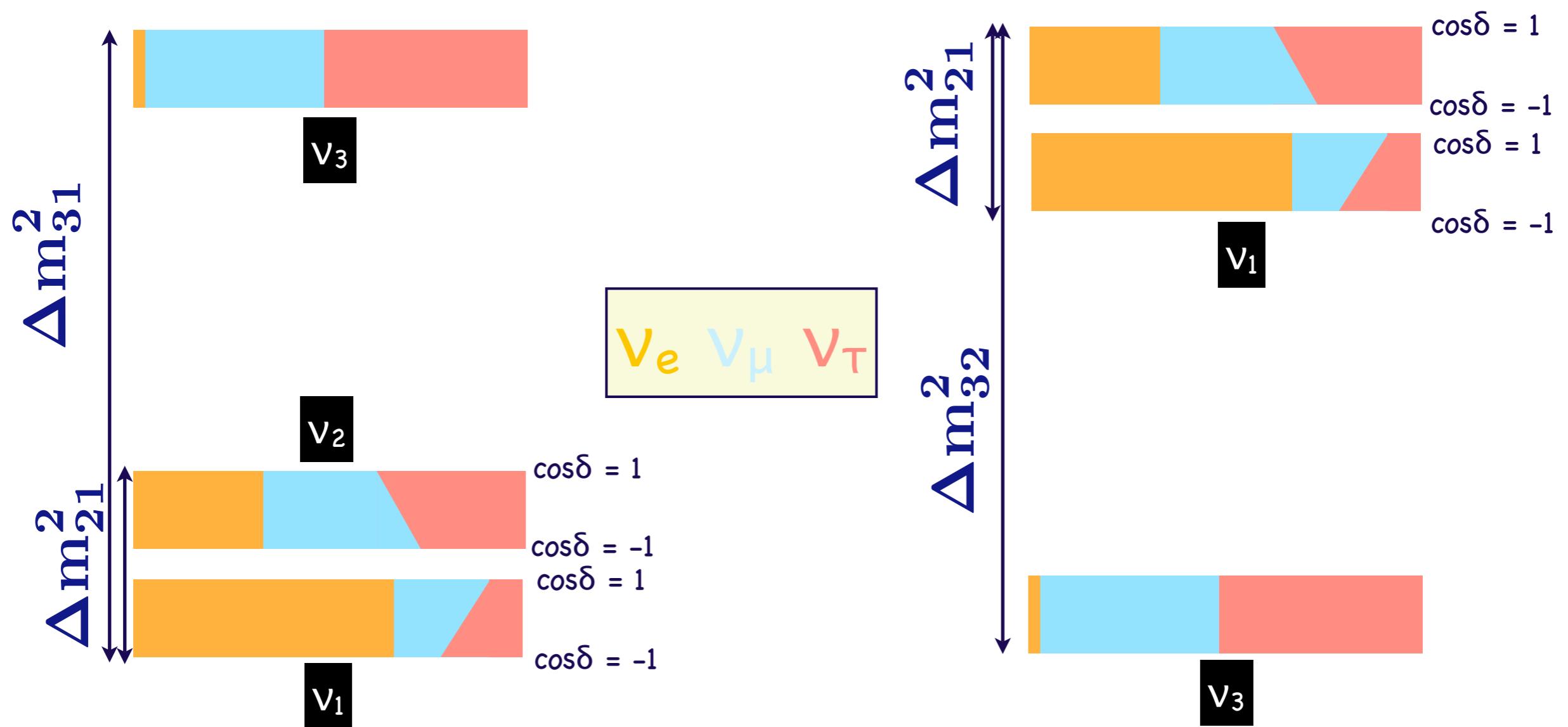
$$c_{ij} \equiv \cos \theta_{ij} \quad s_{ij} \equiv \sin \theta_{ij} \quad \theta_{ij} \in [0, \pi/2] \quad \delta \in [0, 2\pi] \quad \alpha_i \in [0, 2\pi]$$

known : θ_{23} θ_{13} θ_{12}

unknown : δ α_2 α_3

A Successful Scenario

The Squared Mass Spectrum



Normal Ordering

Ordering not known !

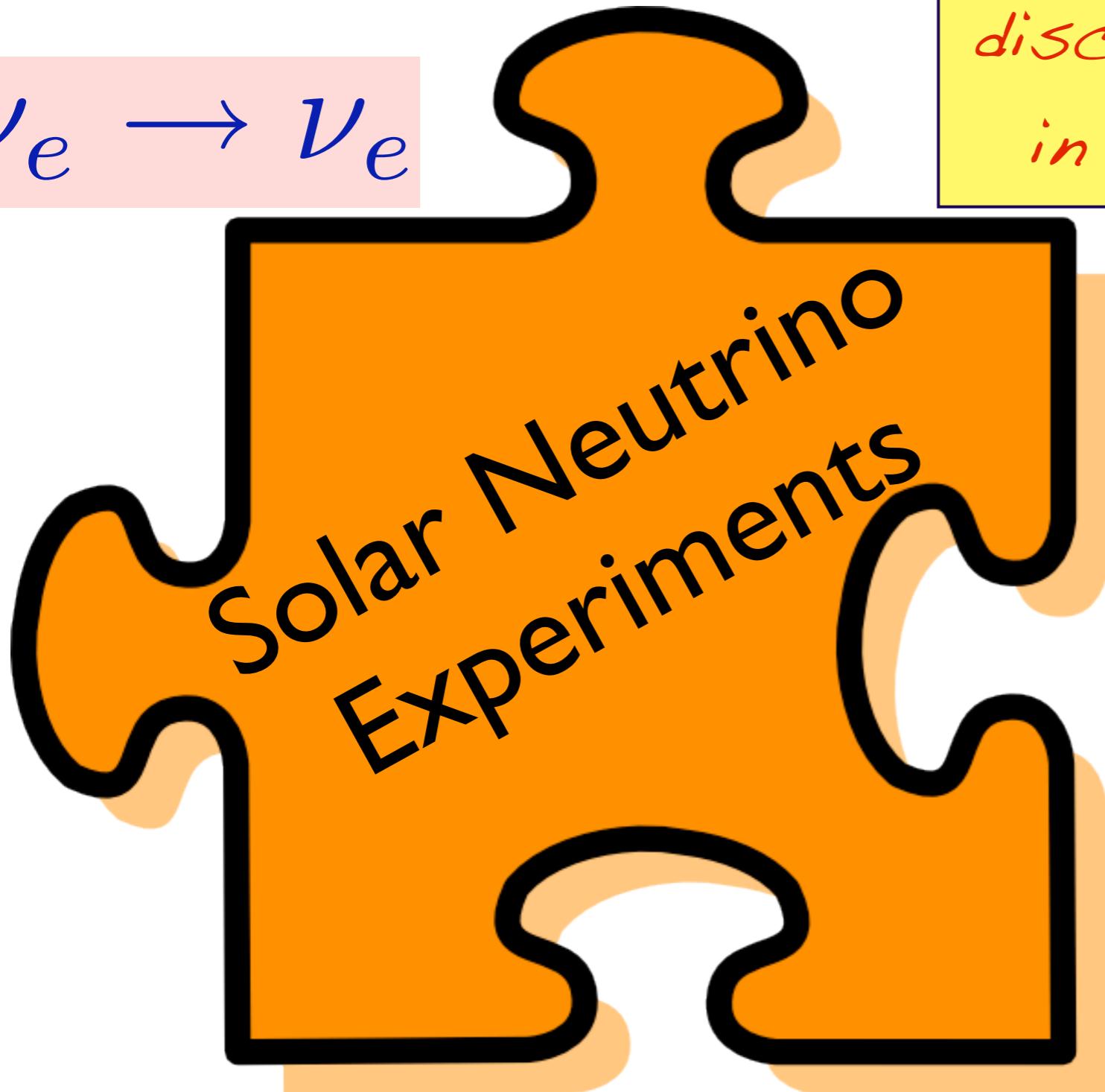
Inverse Ordering



FROM DISCOVERY TO
PRECISION

Data: Pieces of the Puzzle

$$\nu_e \rightarrow \nu_e$$



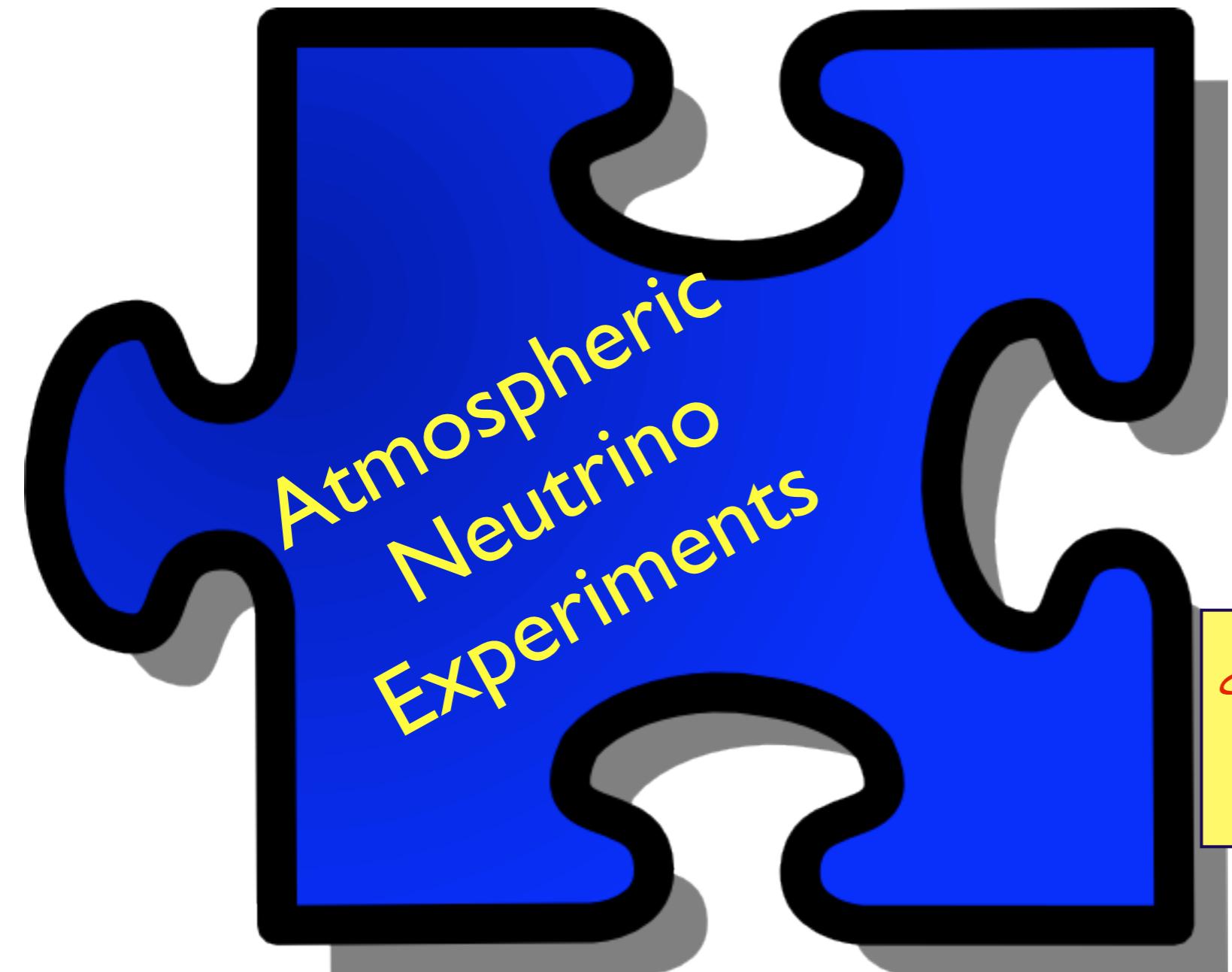
discovered oscillations
in vacuum & matter

Chlorine
Gallex/GNO
SAGE
SKI-SK2-Sk3-SK4
SNO
Borexino

$$\Delta m_{21}^2$$

$$\sin^2 \theta_{21}$$

Data: Pieces of the Puzzle



$$\nu_\mu \rightarrow \nu_\mu$$
$$\nu_e \rightarrow \nu_e$$

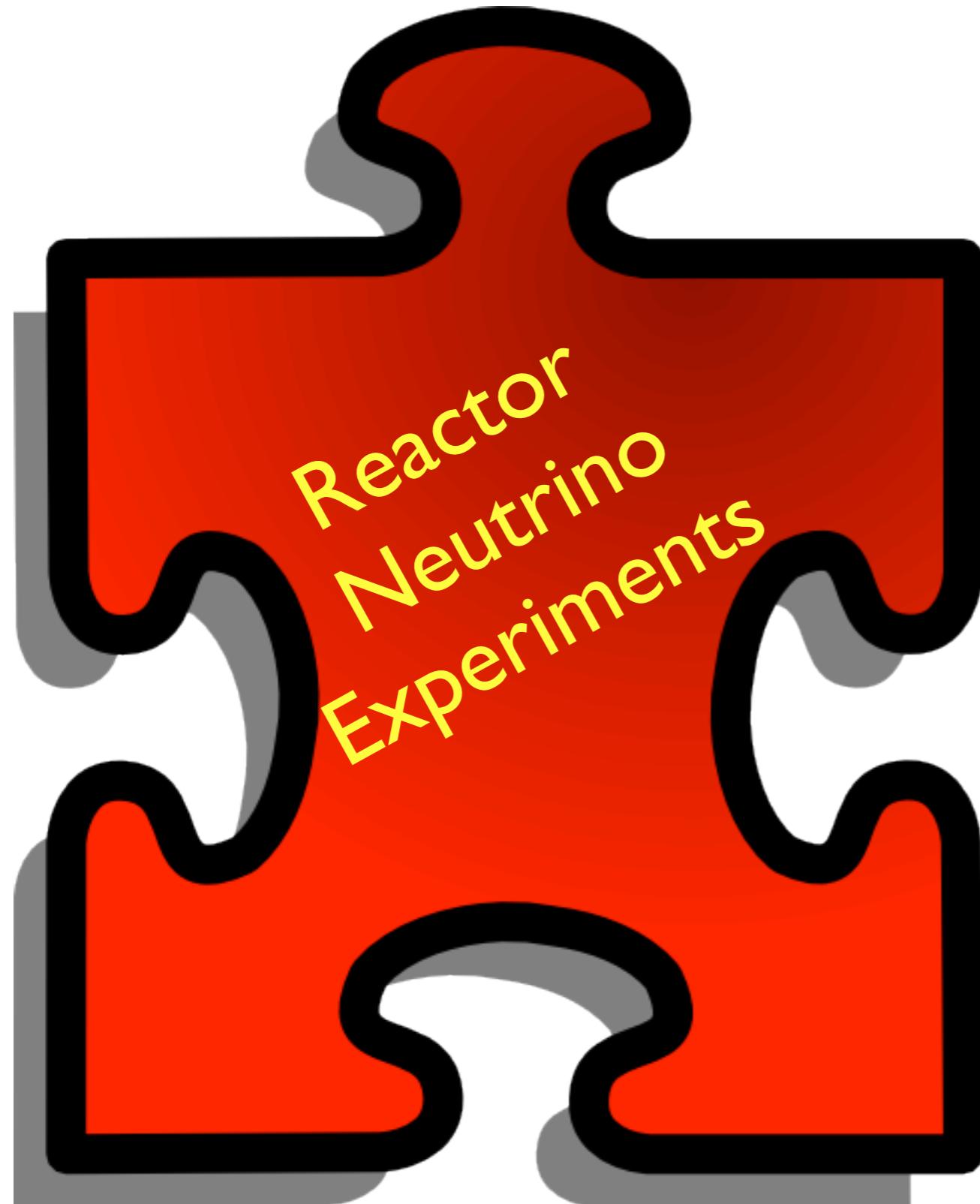
SK1-SK2-Sk3-SK4

discovered oscillations
in vacuum

$$\Delta m_{3\ell}^2$$

$$\sin^2 \theta_{23}$$

Data: Pieces of the Puzzle



$$\nu_e \rightarrow \nu_e$$

KamLAND
CHOOZ/Palo-Verde
Double-CHOOZ
Daya-Bay
Reno

discovered oscillations in vacuum

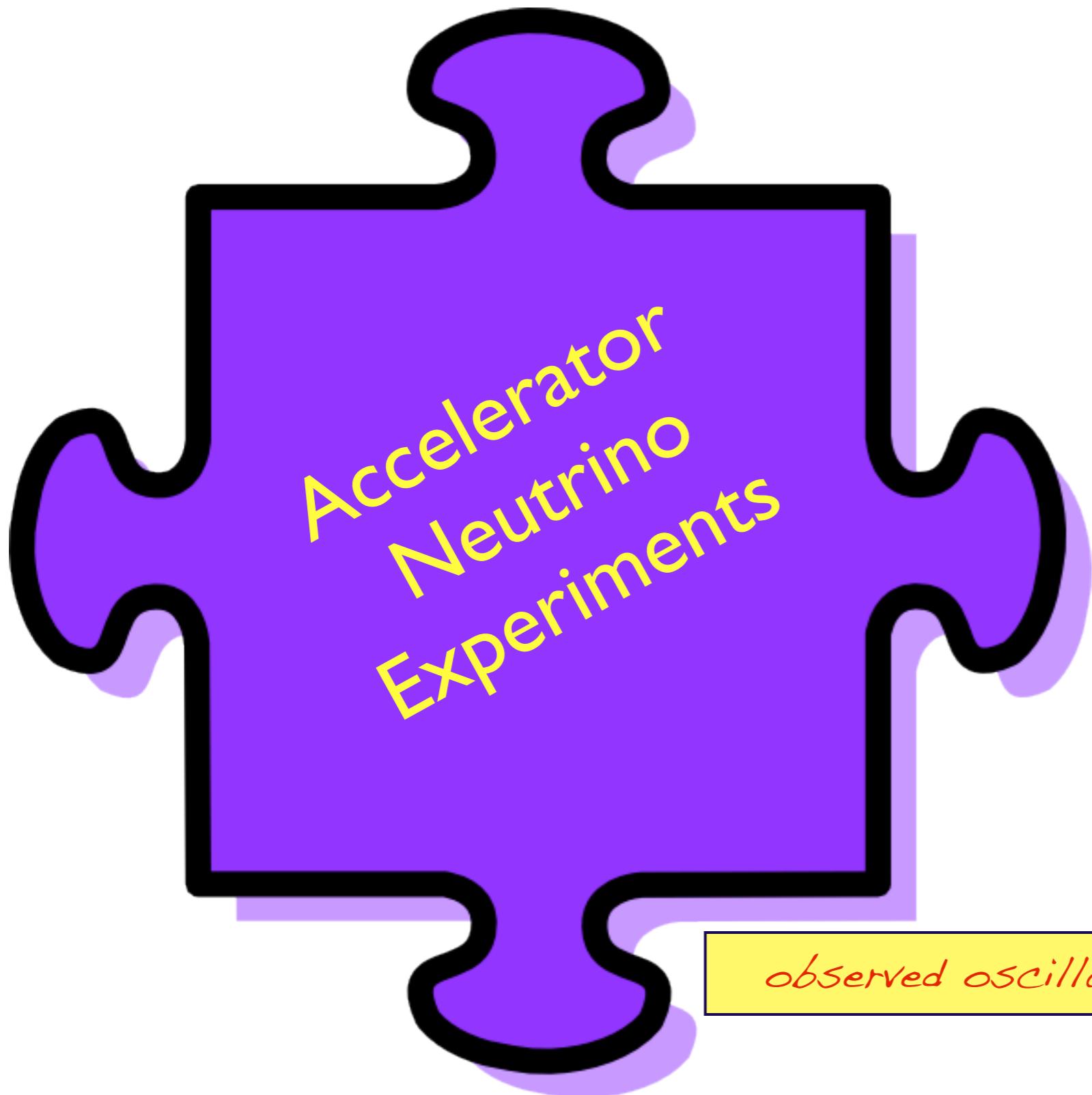
$$\Delta m_{21}^2$$

 $\sin^2 \theta_{21}$

$$\Delta m_{3\ell}^2$$

 $\sin^2 \theta_{13}$

Data: Pieces of the Puzzle



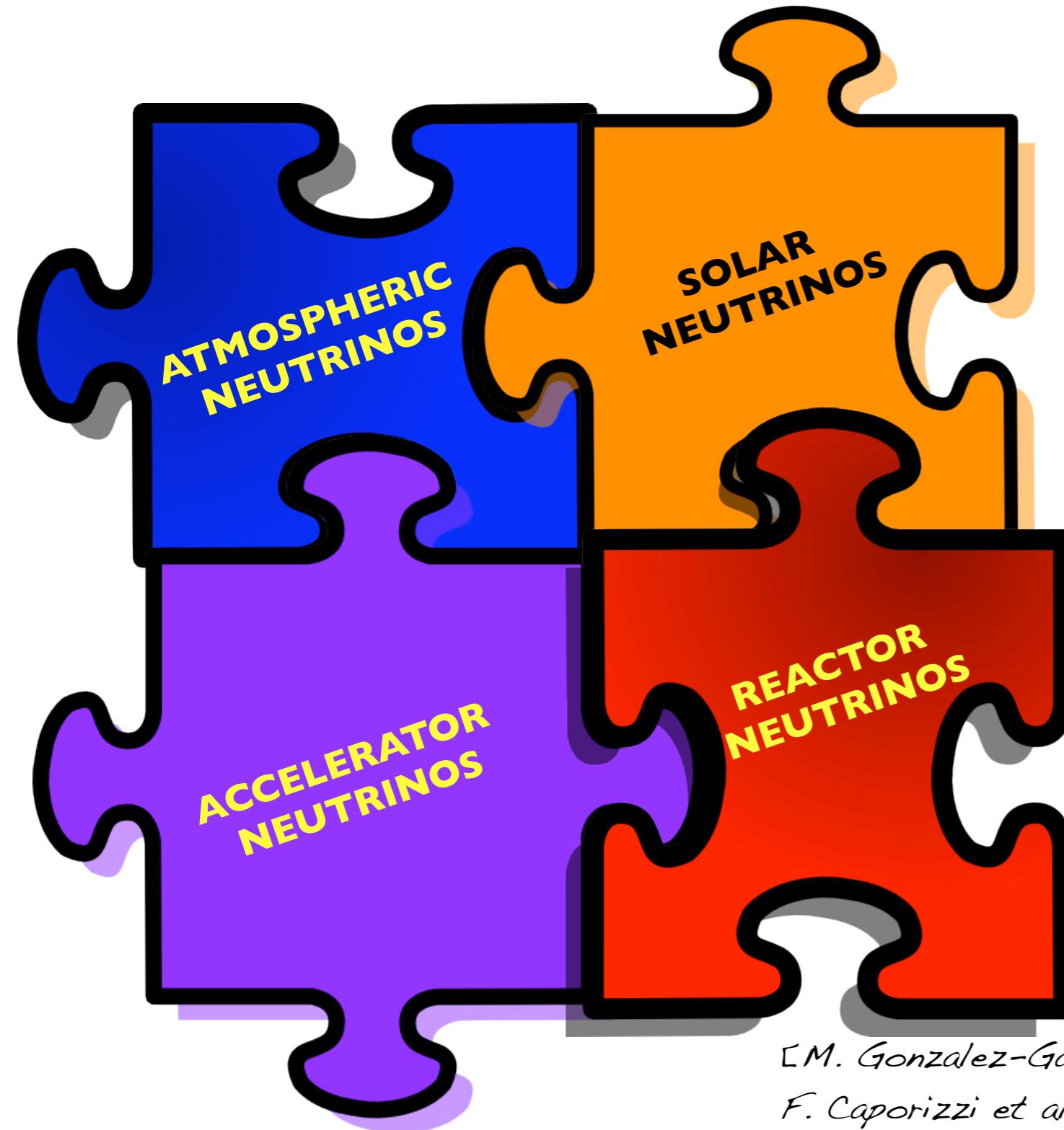
$$\nu_\mu \rightarrow \nu_\mu$$
$$\nu_\mu \rightarrow \nu_e$$
$$\nu_\mu \rightarrow \nu_\tau$$

K₂K
MINOS
T₂K
OPERA
(+ Nova)

observed oscillations

$$\Delta m_{3\ell}^2 \quad \sin^2 \theta_{13}$$
$$\sin^2 \theta_{23}$$

Global Analyses



by combining data we can

Find Best Estimates

Test Consistency of the Framework

Find Correlations

Find hints on unknown parameters

Useful for guidance

[M. Gonzalez-Garcia et al. arXiv:1409.5439 & arXiv:1507.04366 ;
F. Capozzi et al. arXiv:1312.2878; D. Forero et al. arXiv:1405.7540]



$$\Delta m_{21}^2$$

$$\sin^2 \theta_{21}$$

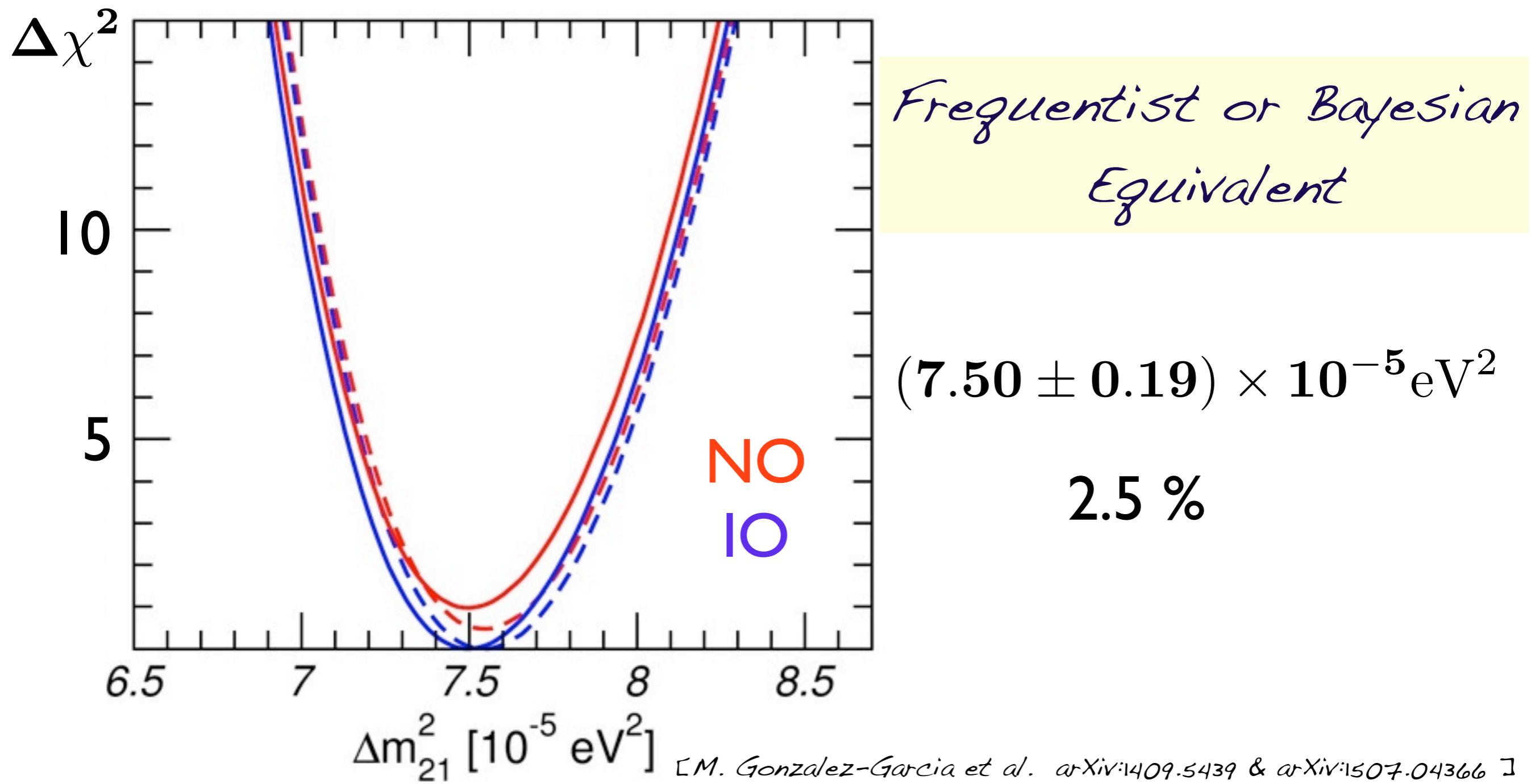
$$|\Delta m_{3\ell}^2|$$

$$\sin^2 \theta_{13}$$

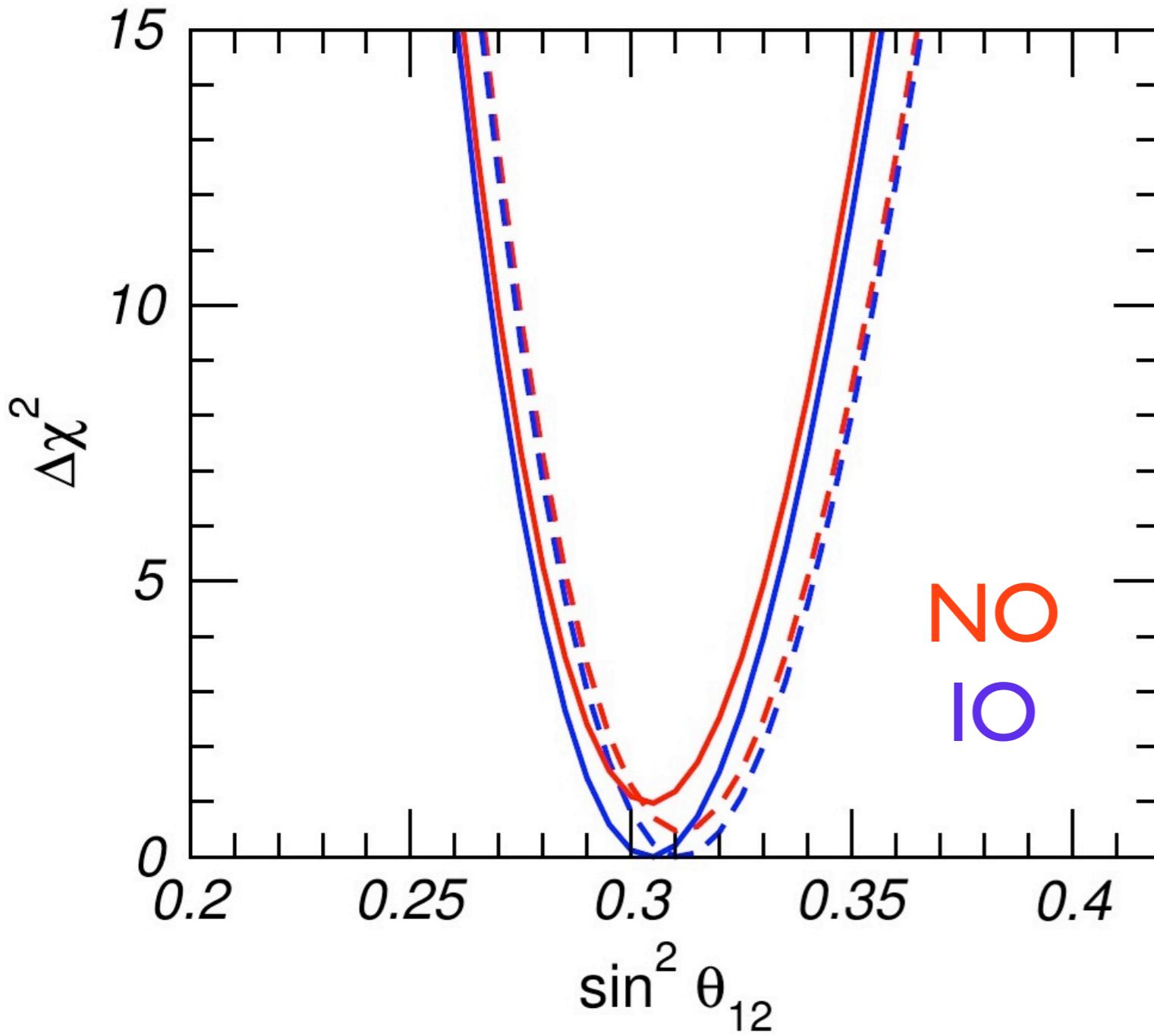
ROBUST MEASUREMENTS

Δm_{21}^2

NuFIT 2.0 (2014)



$$\sin^2 \theta_{21}$$



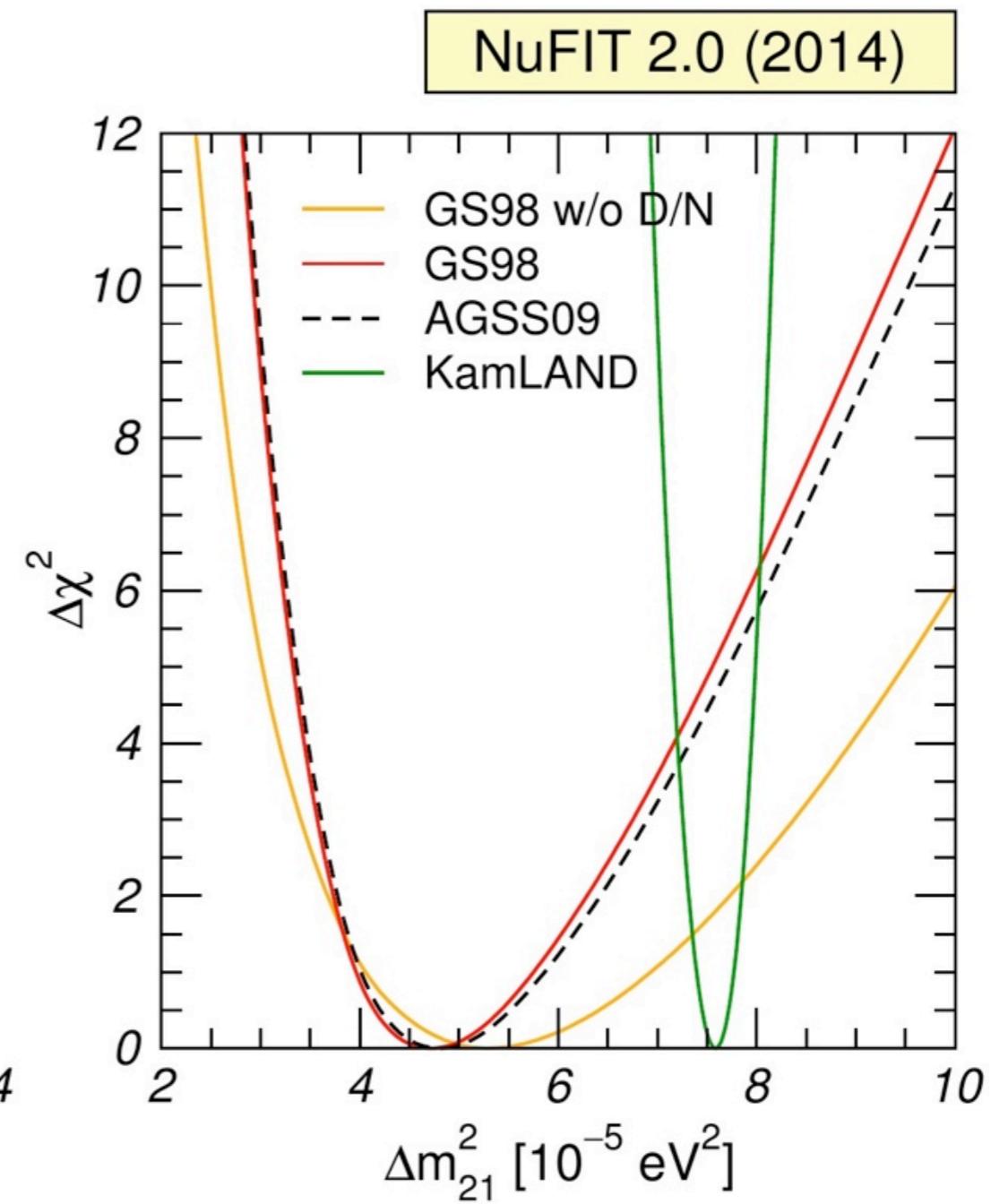
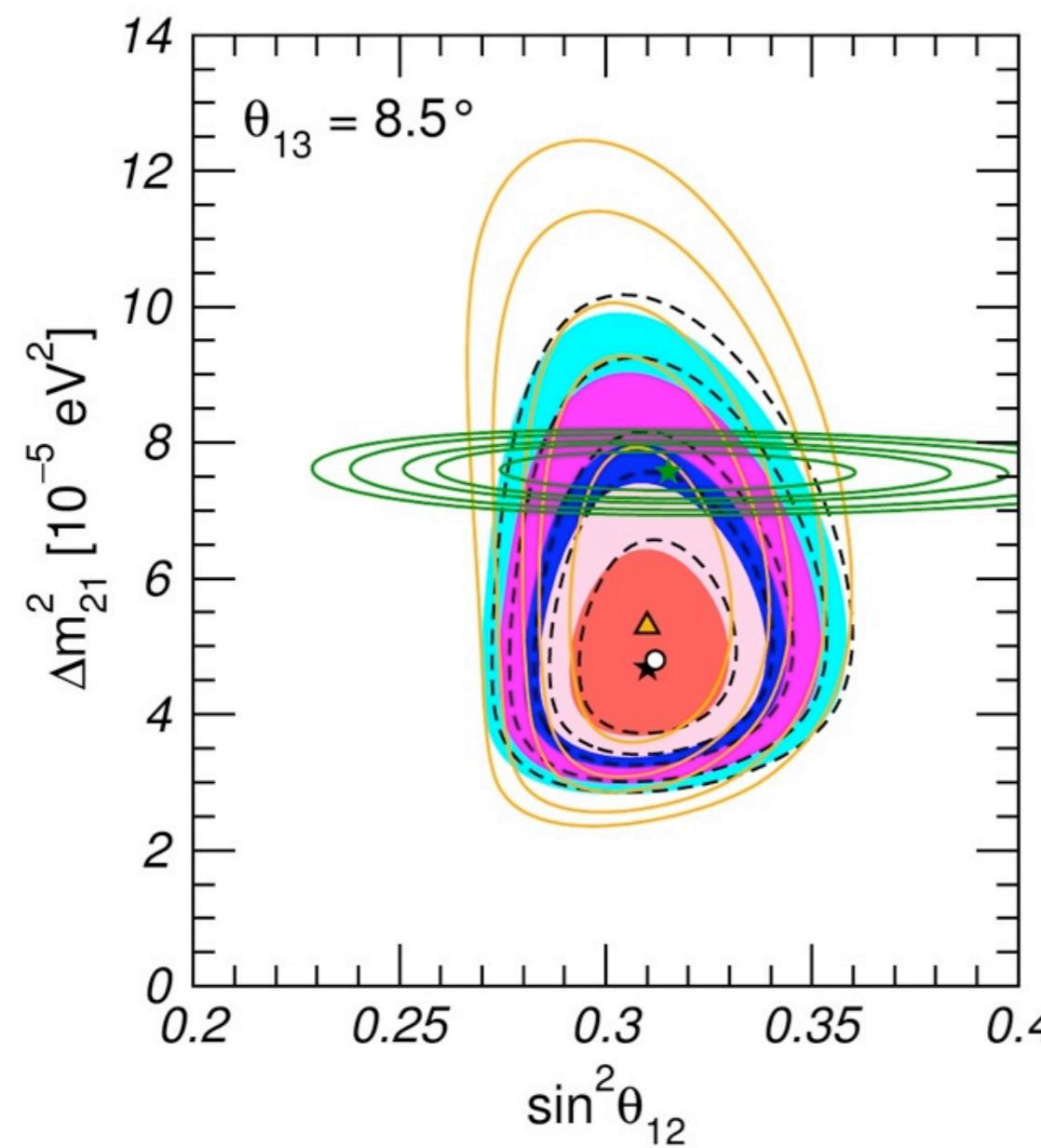
Frequentist or Bayesian
Equivalent

0.304 ± 0.013

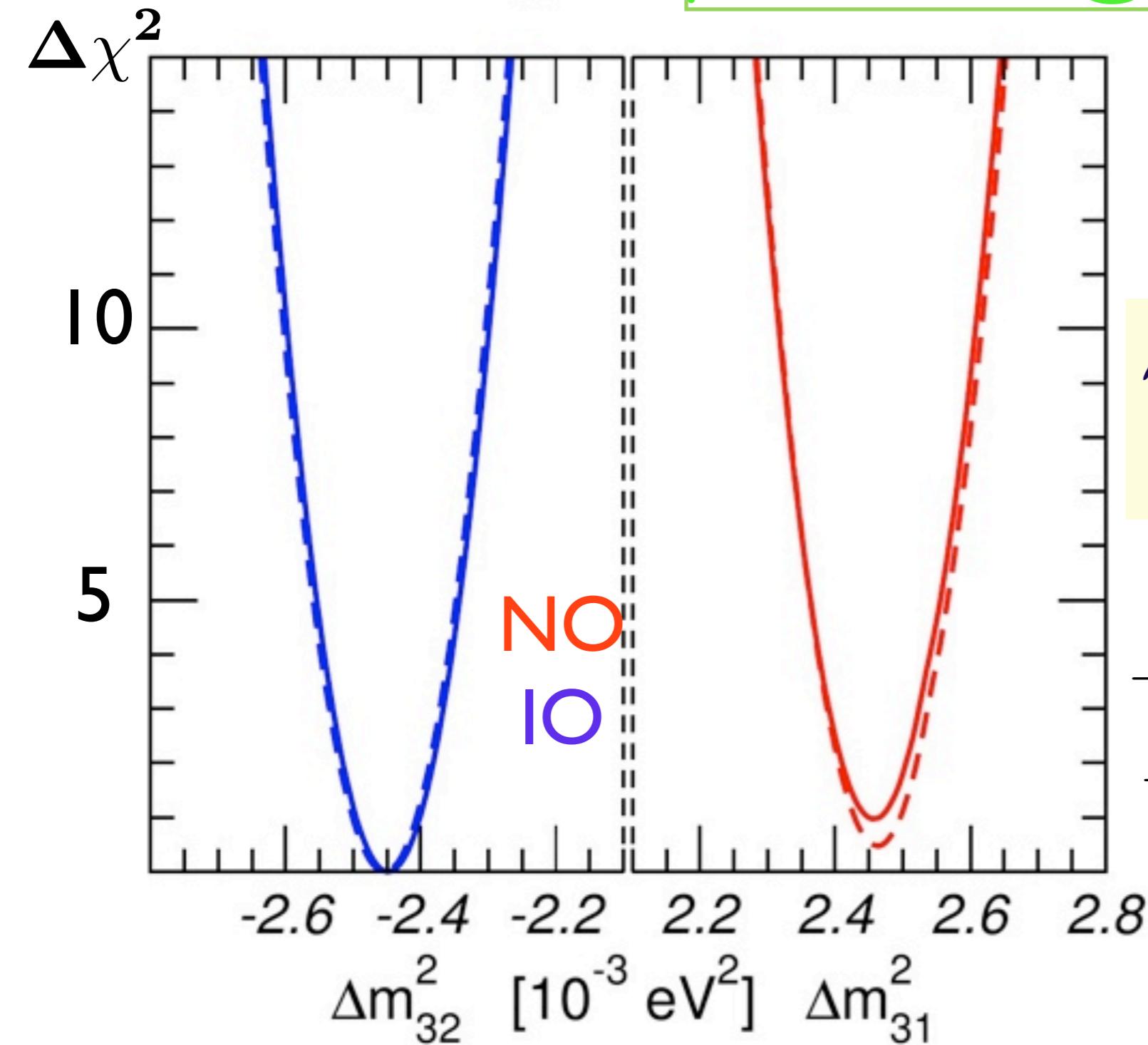
4.3 %

Δm_{21}^2

Tension between Solar and KamLAND



$$\Delta m_{3\ell}^2$$



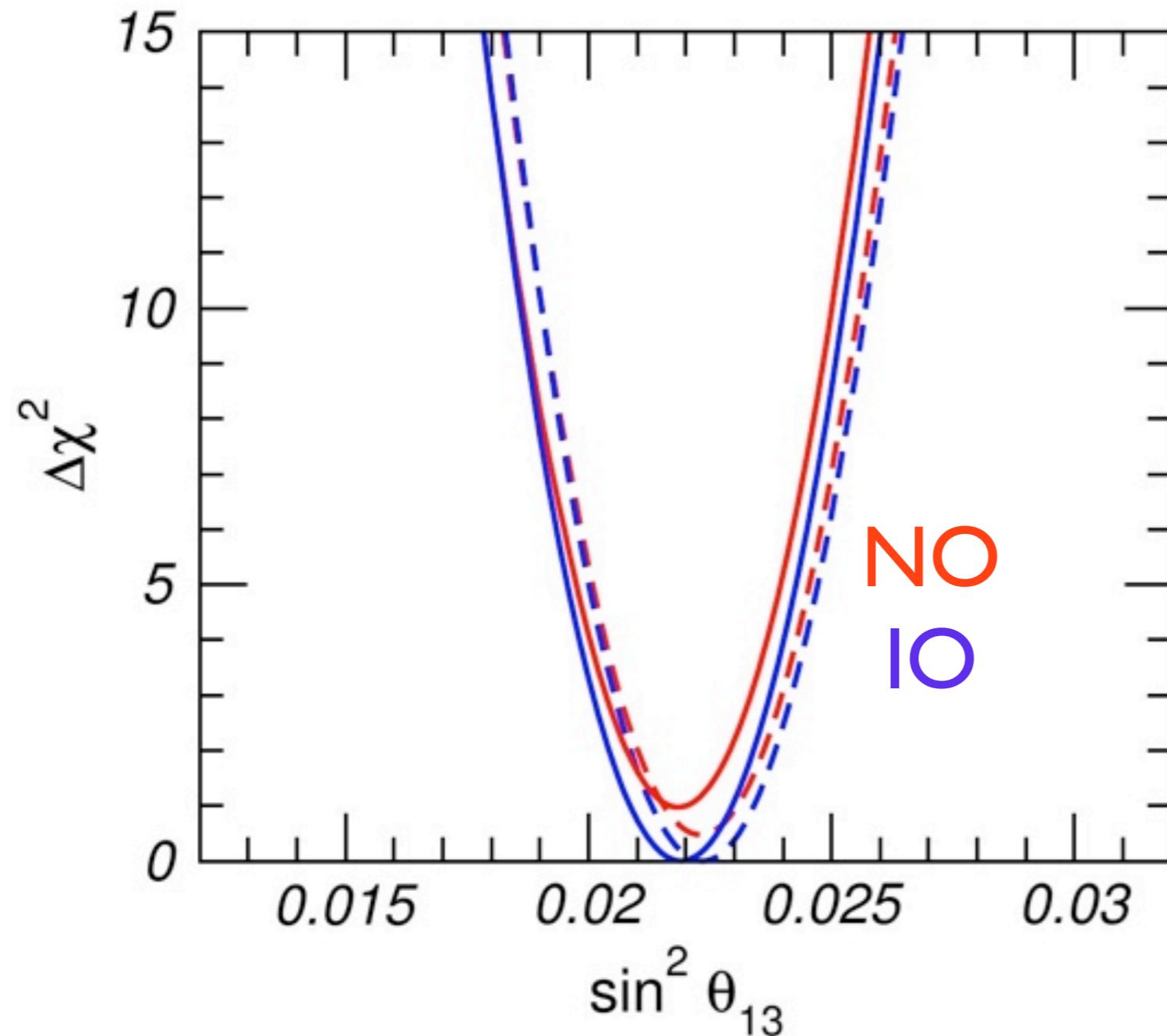
Frequentist or Bayesian
Equivalent

$$+ (2.457 \pm 0.047) \times 10^{-3} \text{ eV}^2$$

$$- (2.449 \pm 0.047) \times 10^{-3} \text{ eV}^2$$

1.9 %

$$\sin^2 \theta_{13}$$



Frequentist or Bayesian
Equivalent

$$0.0218 \pm 0.0010$$

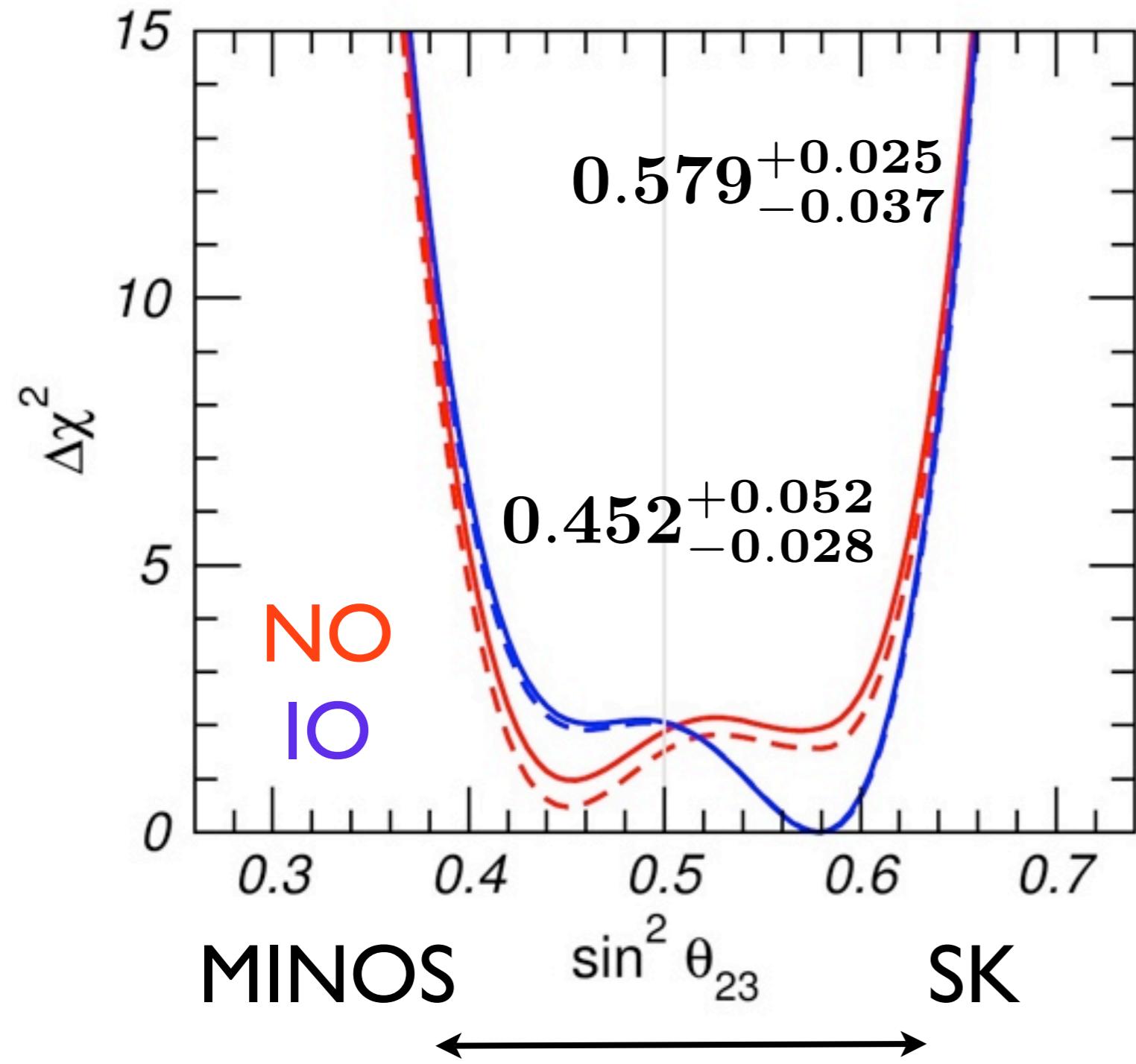
$$4.6\%$$



θ_{23} octant
mass ordering
 δ

HINTS OF AN UNCHARTED
TERRITORY

$$\theta_{23}$$



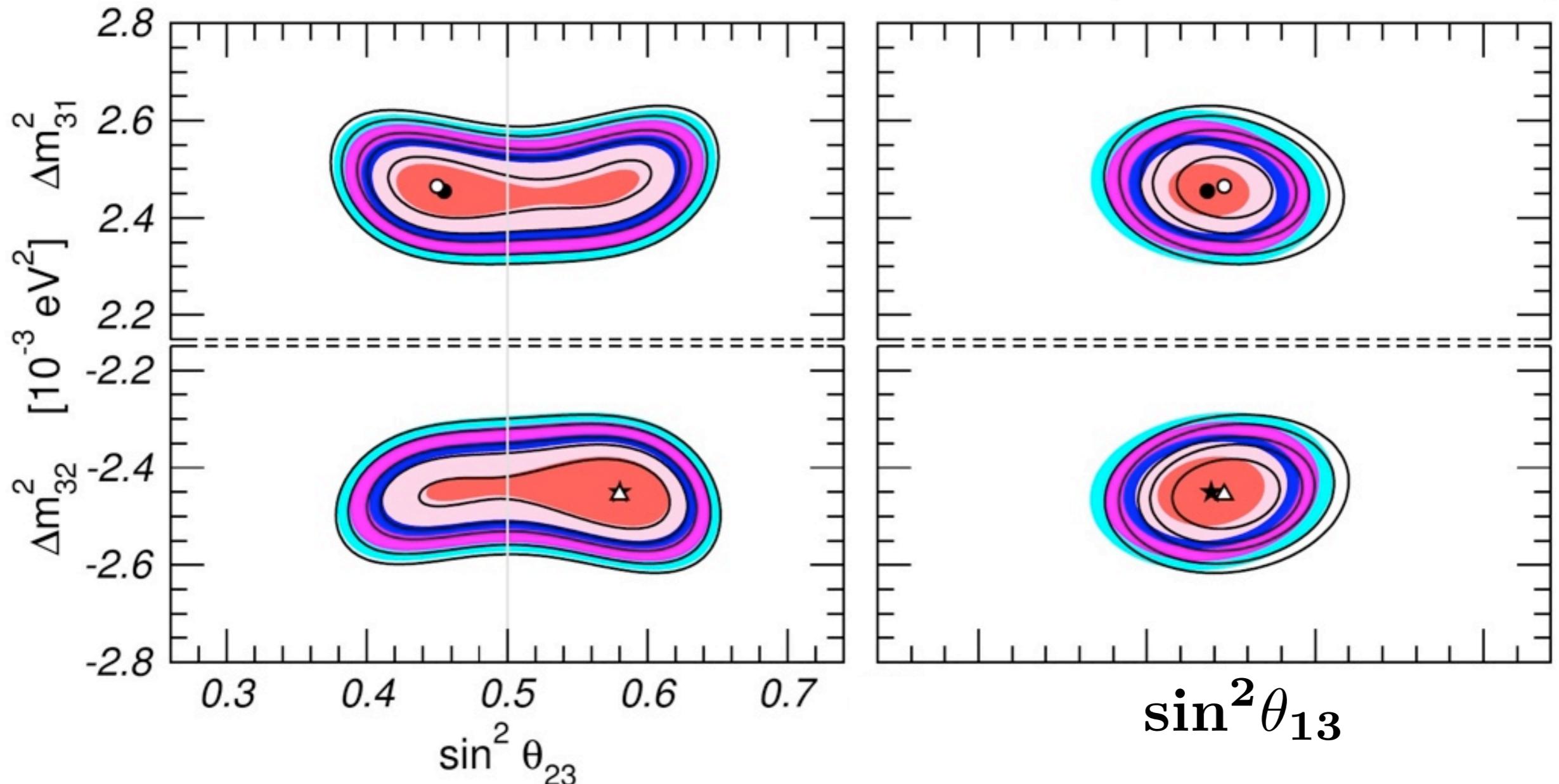
Bayesian Analysis
Weakly Prefer 2nd
(IO)

unstable/fragile

tug-of-war

No Preferred Mass Ordering

NuFIT 2.0 (2014)

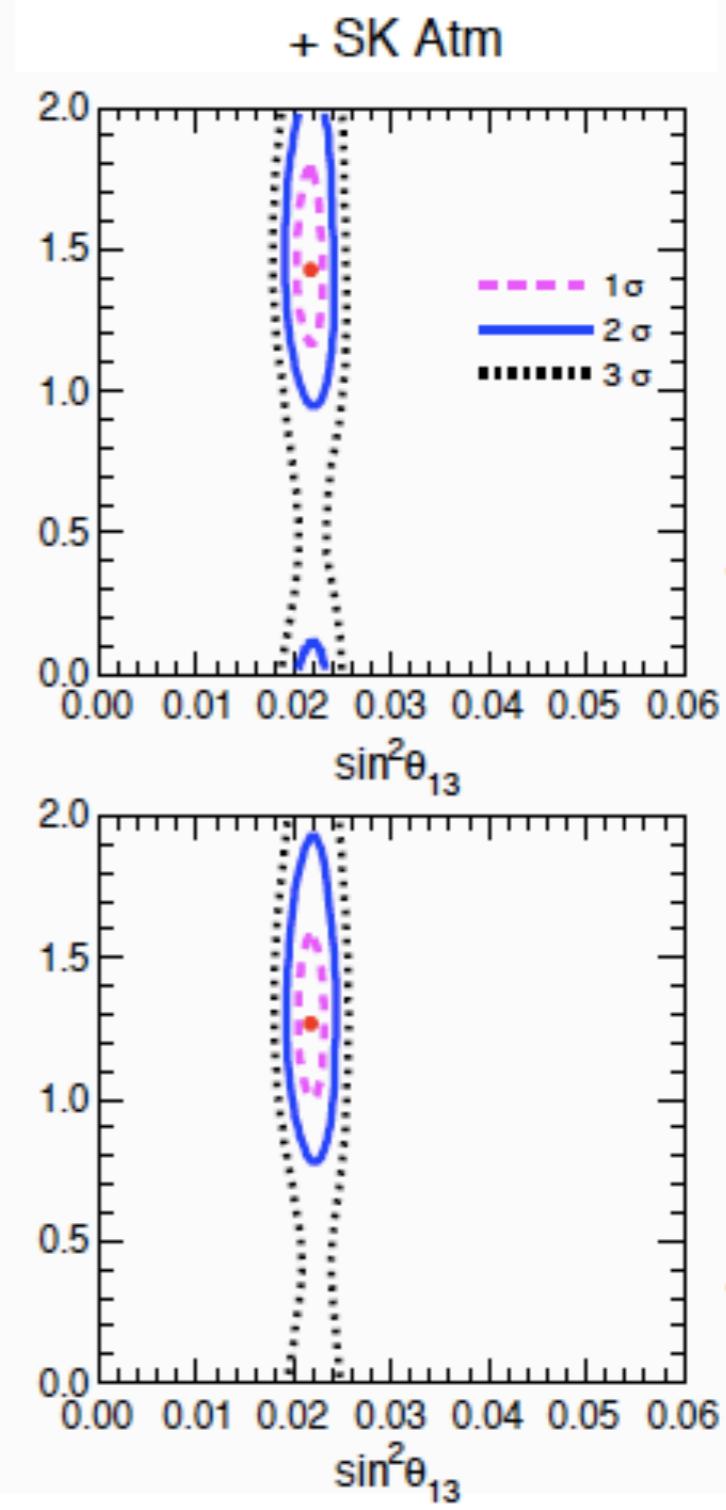
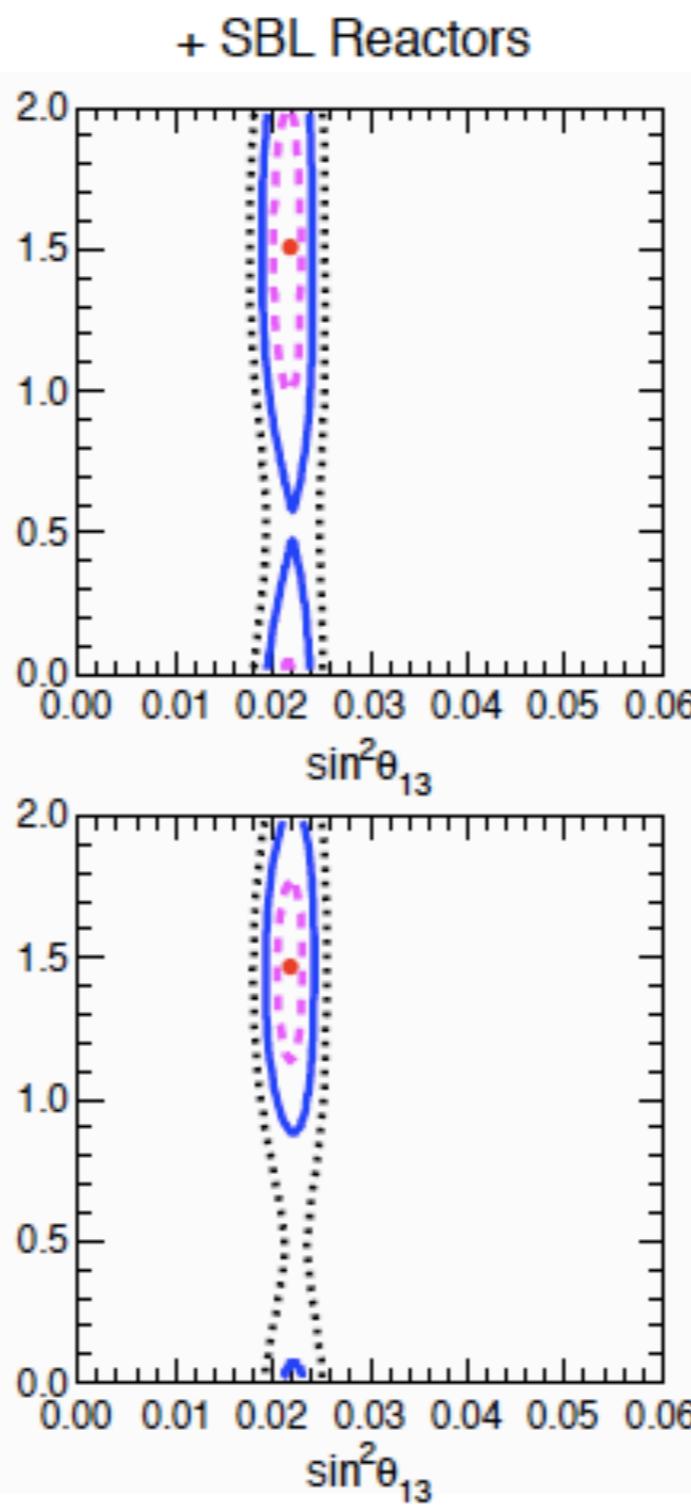
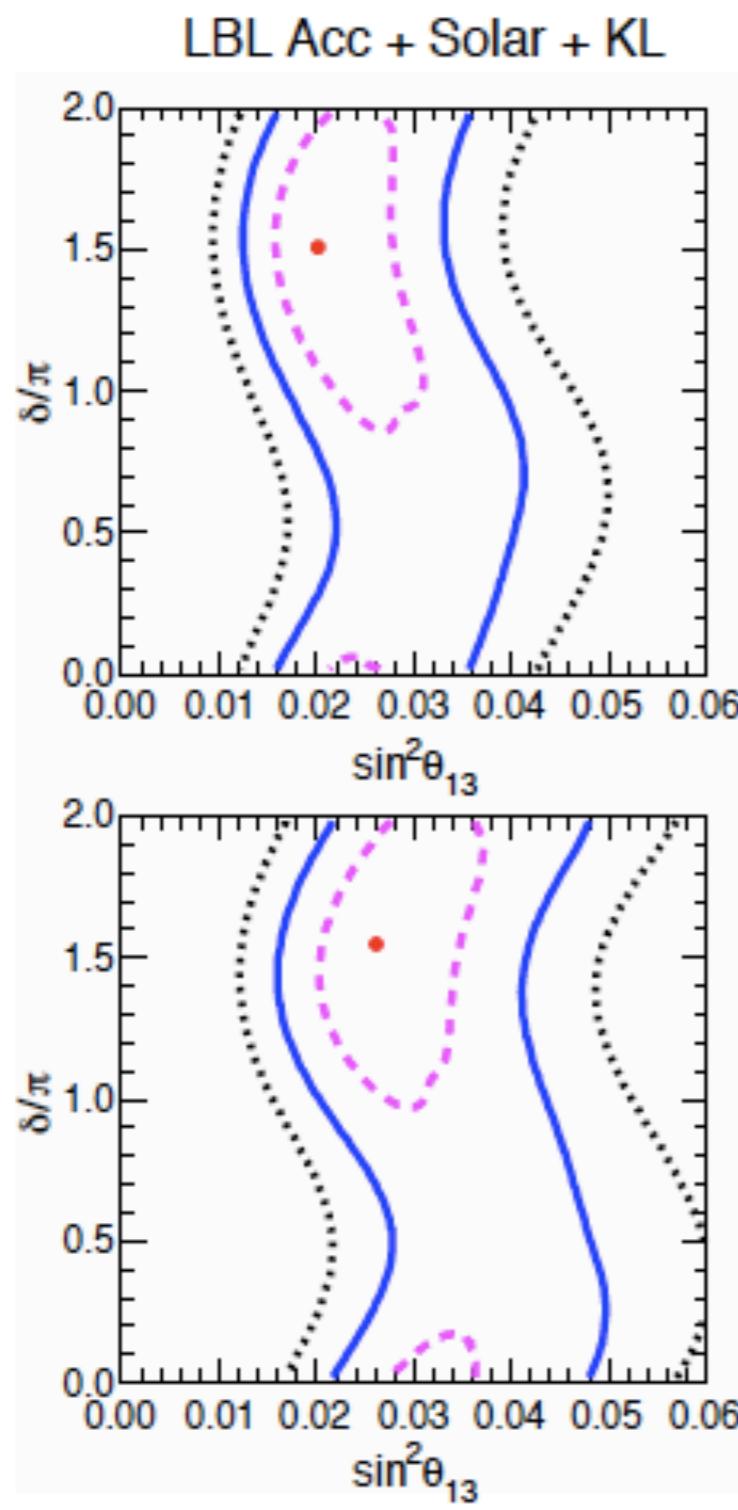


Bayesian Analysis
Weakly Prefer IO
Not Significant

[M. Gonzalez-Garcia et al. arXiv:1507.04366]

$$\delta$$

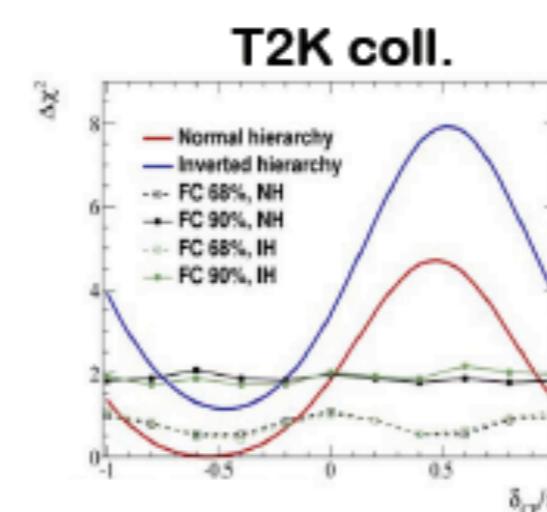
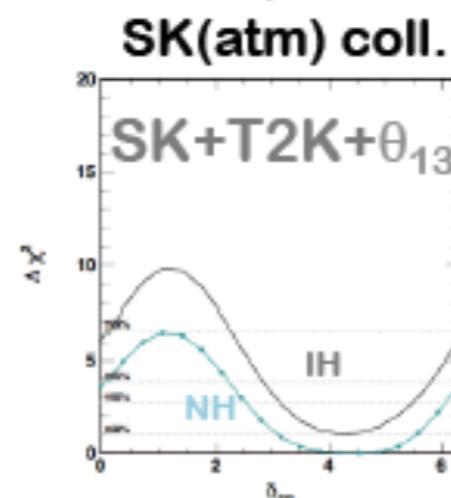
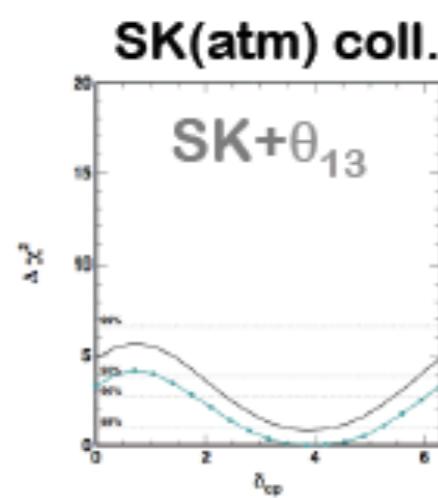
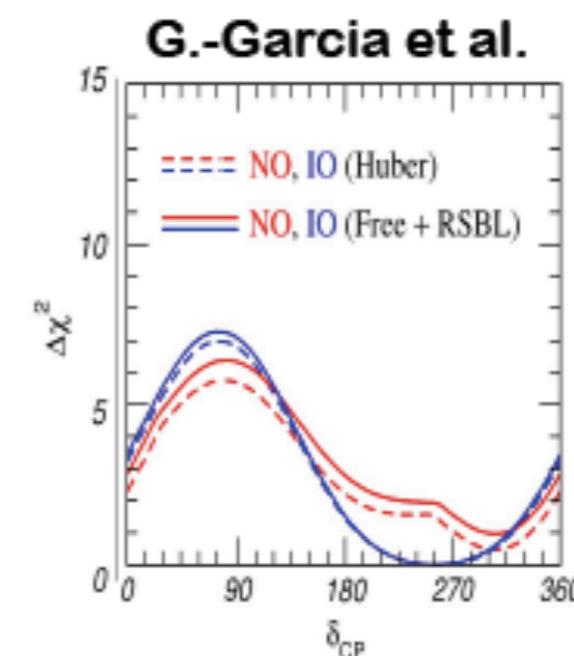
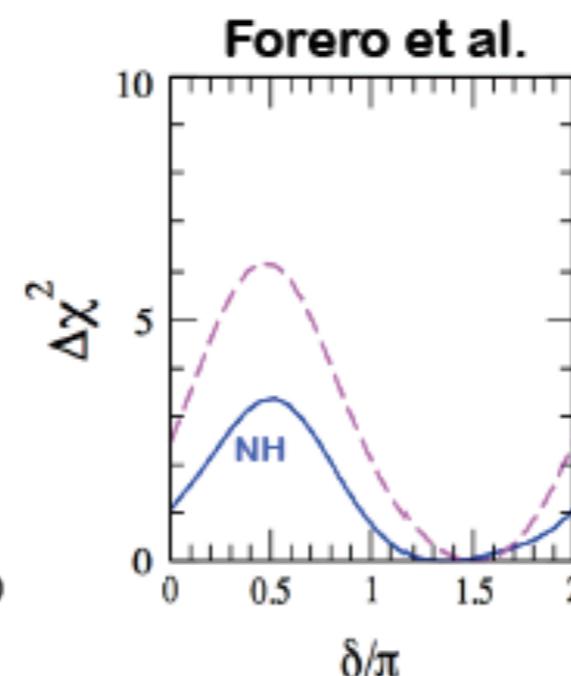
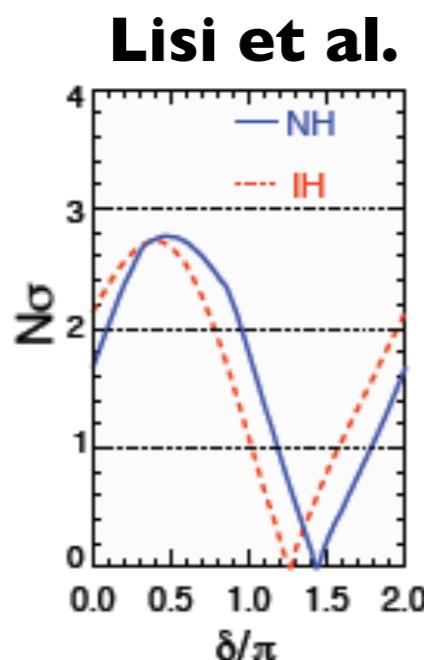
[E. Lisi, Moriond 2015]



δ

[E. Lisi, Moriond 2015]

For comparison:



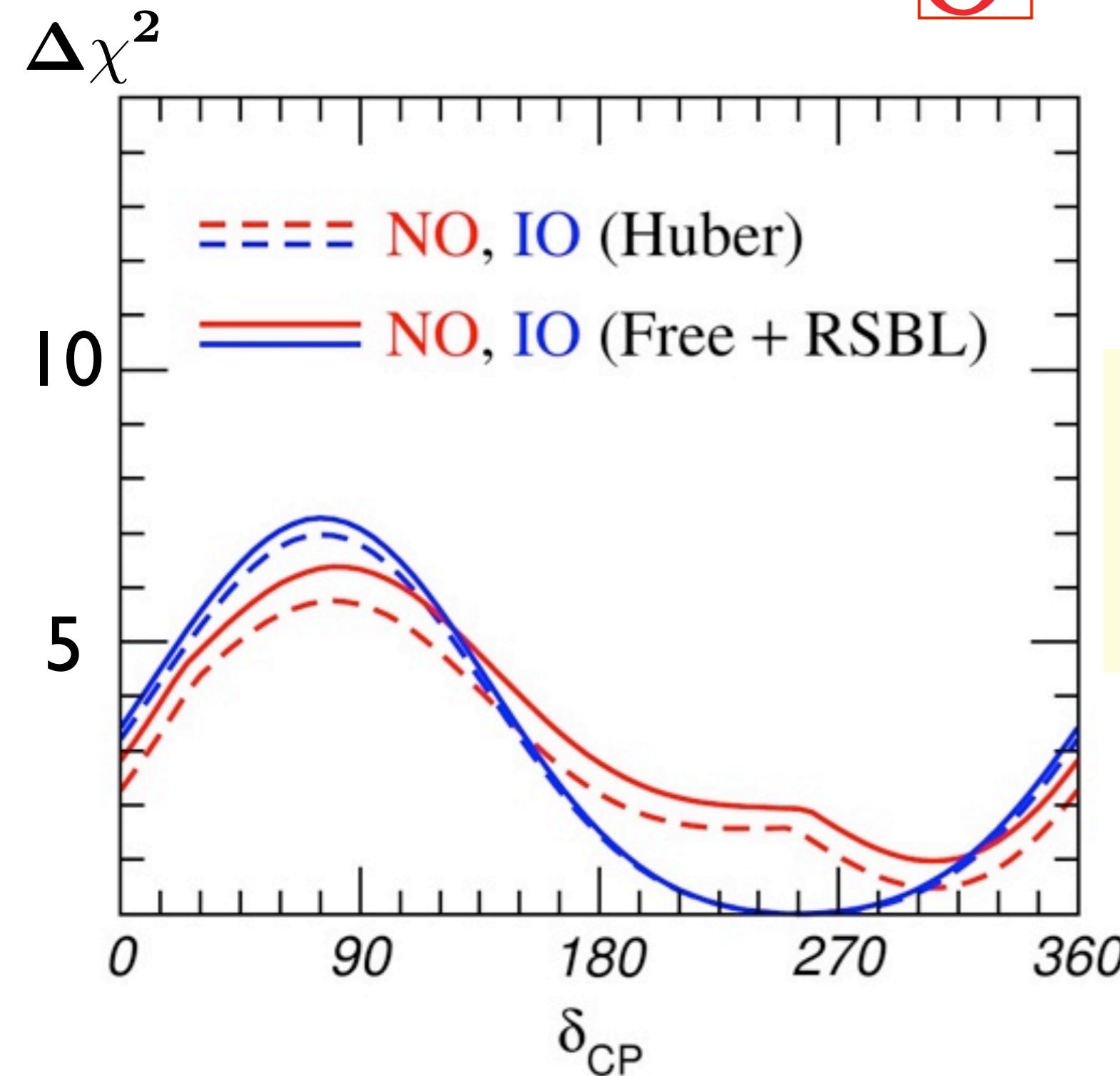
Status of representative CP phase values (in various fits):

$\delta/\pi \sim 3/2$: **preferred** (nearly maximal CPV with $\sin\delta \sim -1$)

$\delta/\pi \sim 1/5$: **disfavored** (by ~2-2.6 sigma w.r.t. to preferred value)

$\delta/\pi \sim 0$ or ~ 1 : **in between** (~1-1.3 sigma away from best fit)

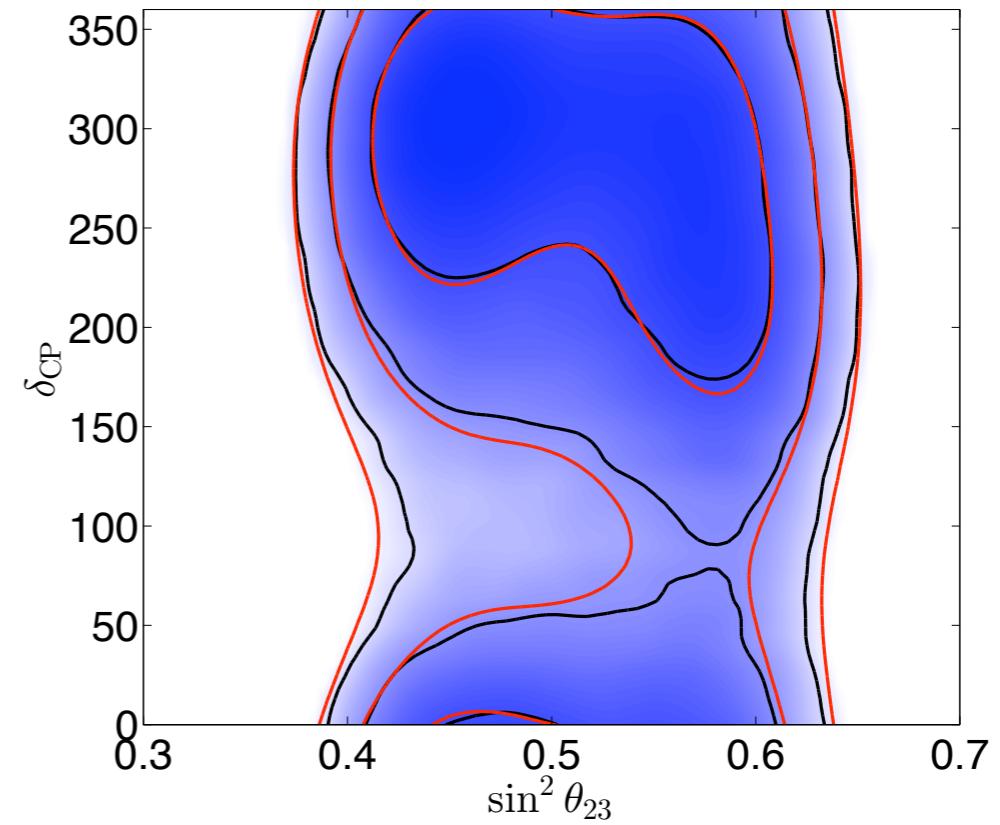
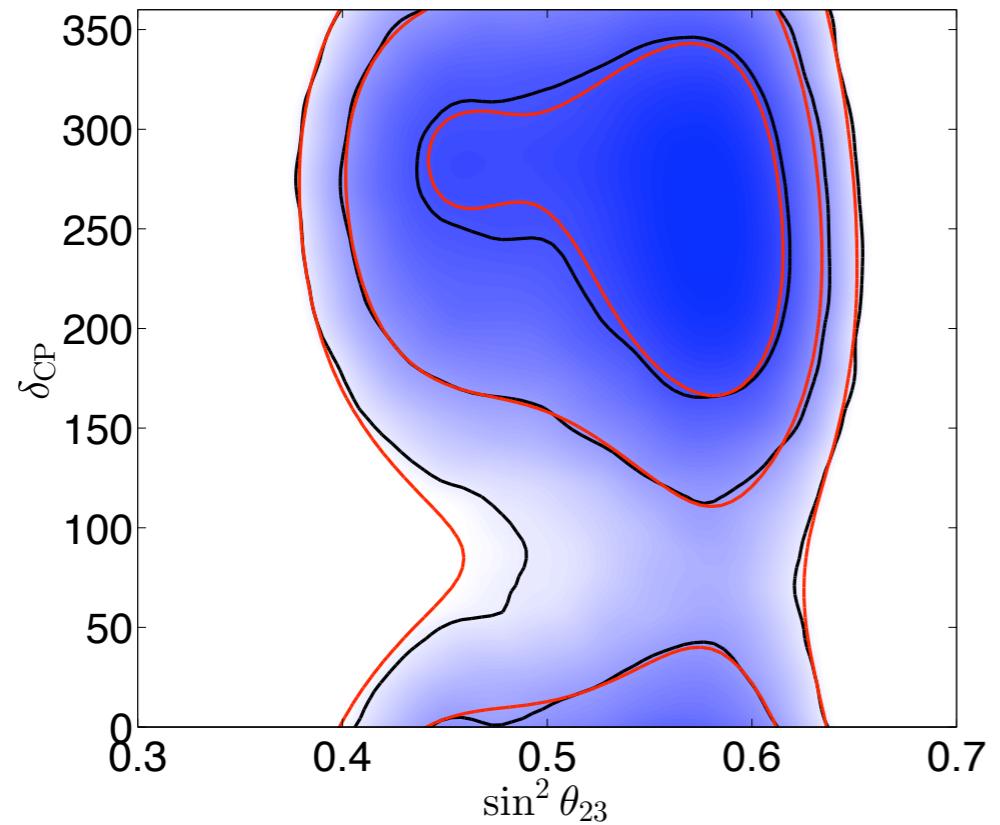
$$\delta$$



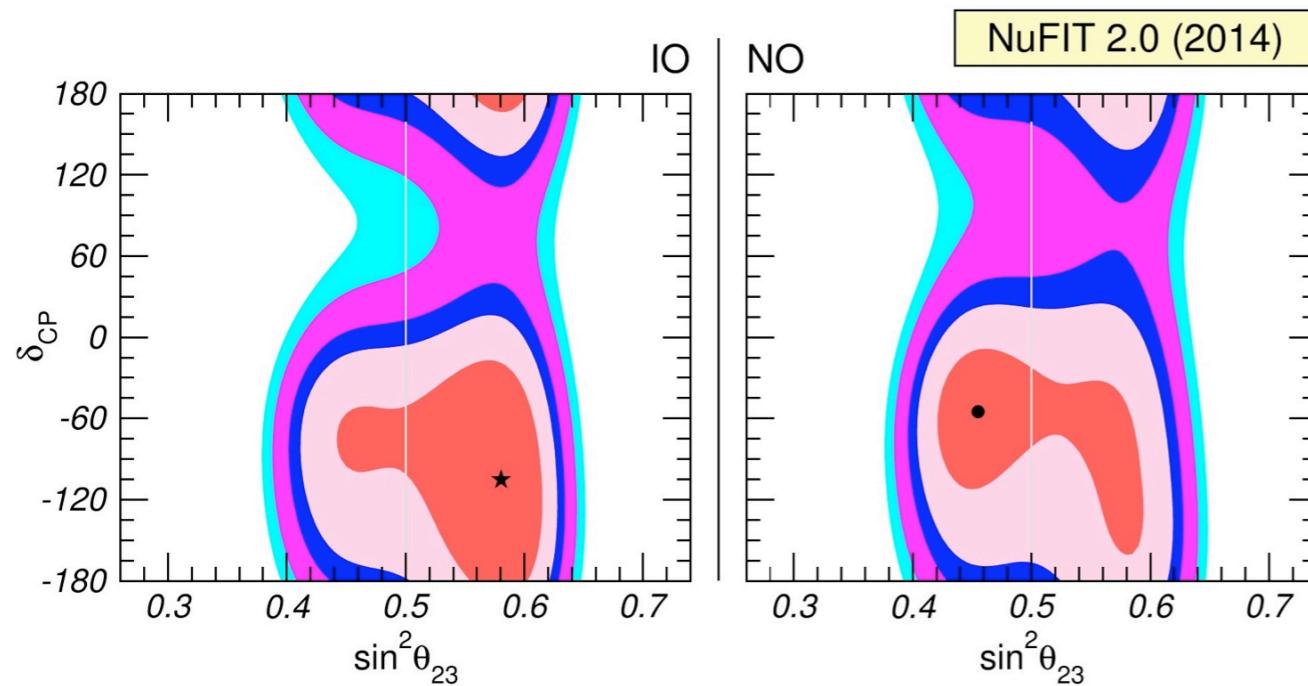
Bayesian Analysis
Prefer CPV over CPC
But Not Significant

IO

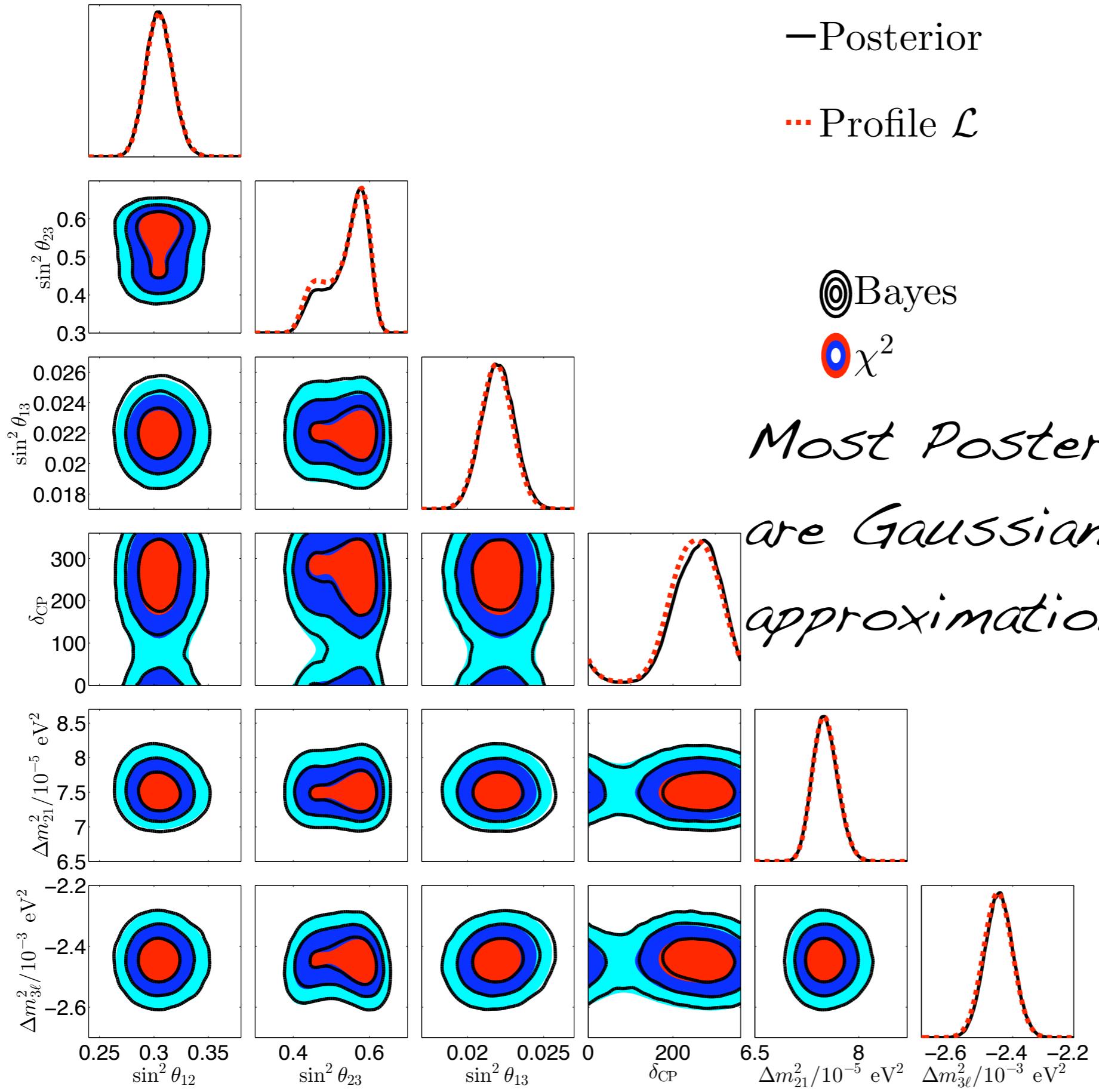
NO



quantitatively stronger in NO



Correlation between
 $\sin^2 \theta_{23} \times \delta$



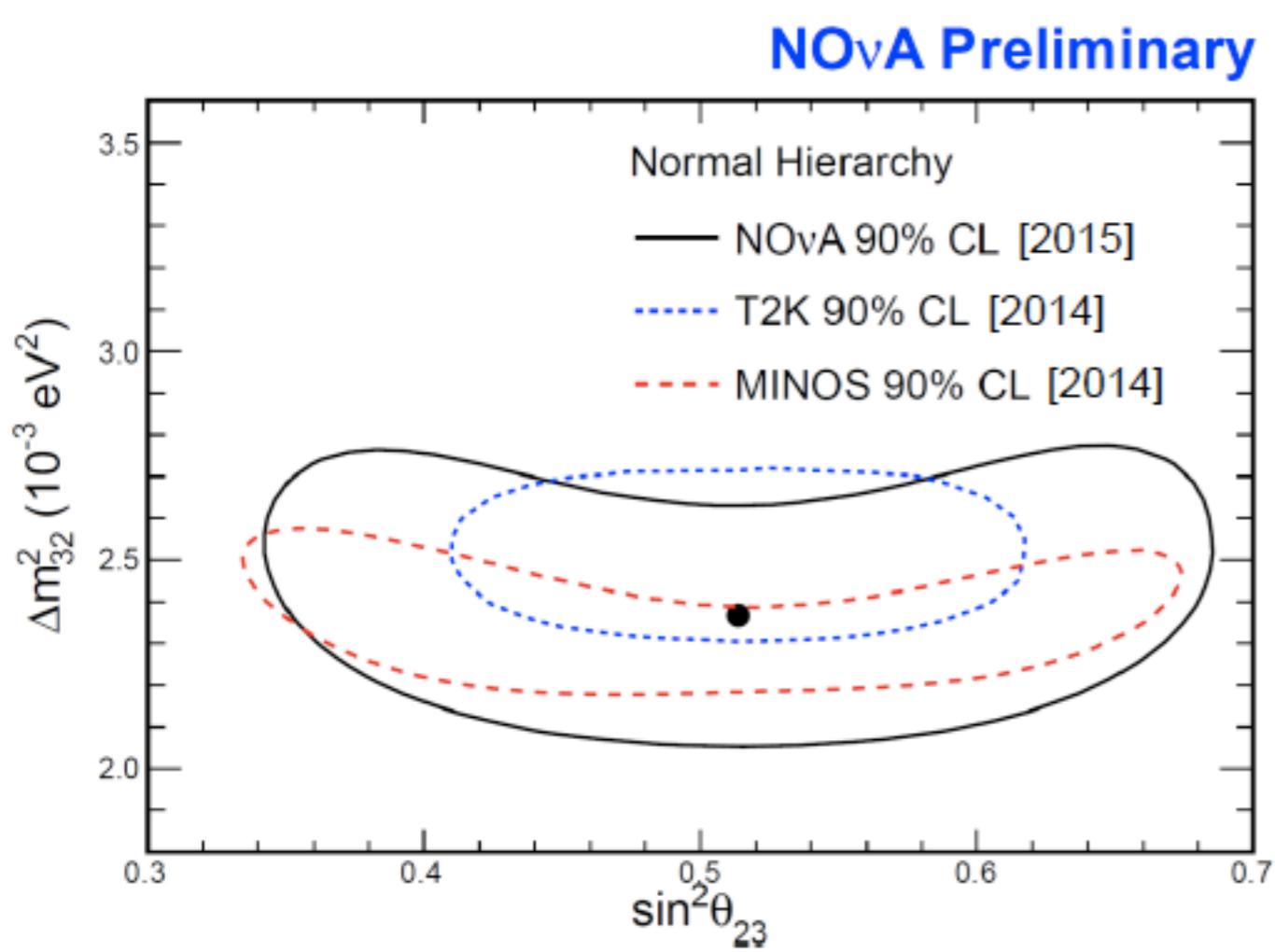
*Most Posterior Distributions
 are Gaussians to a very good
 approximation*



NOVAS DE NOVA

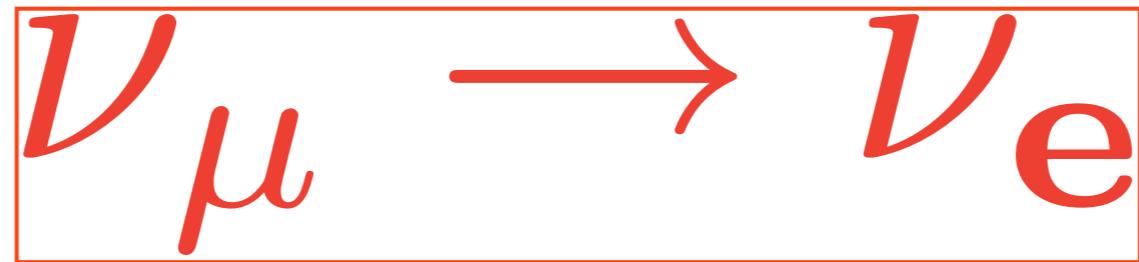
$$\nu_\mu \rightarrow \nu_\mu$$

[R. Patterson, Fermilab JETP Aug. 6, 2015]

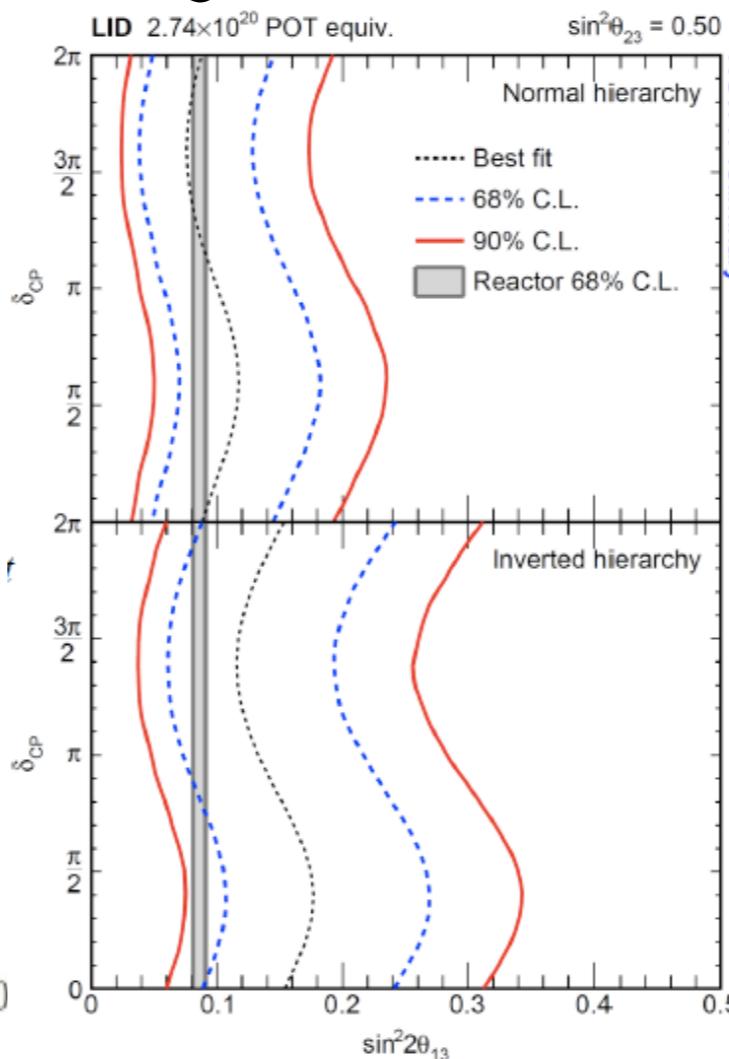
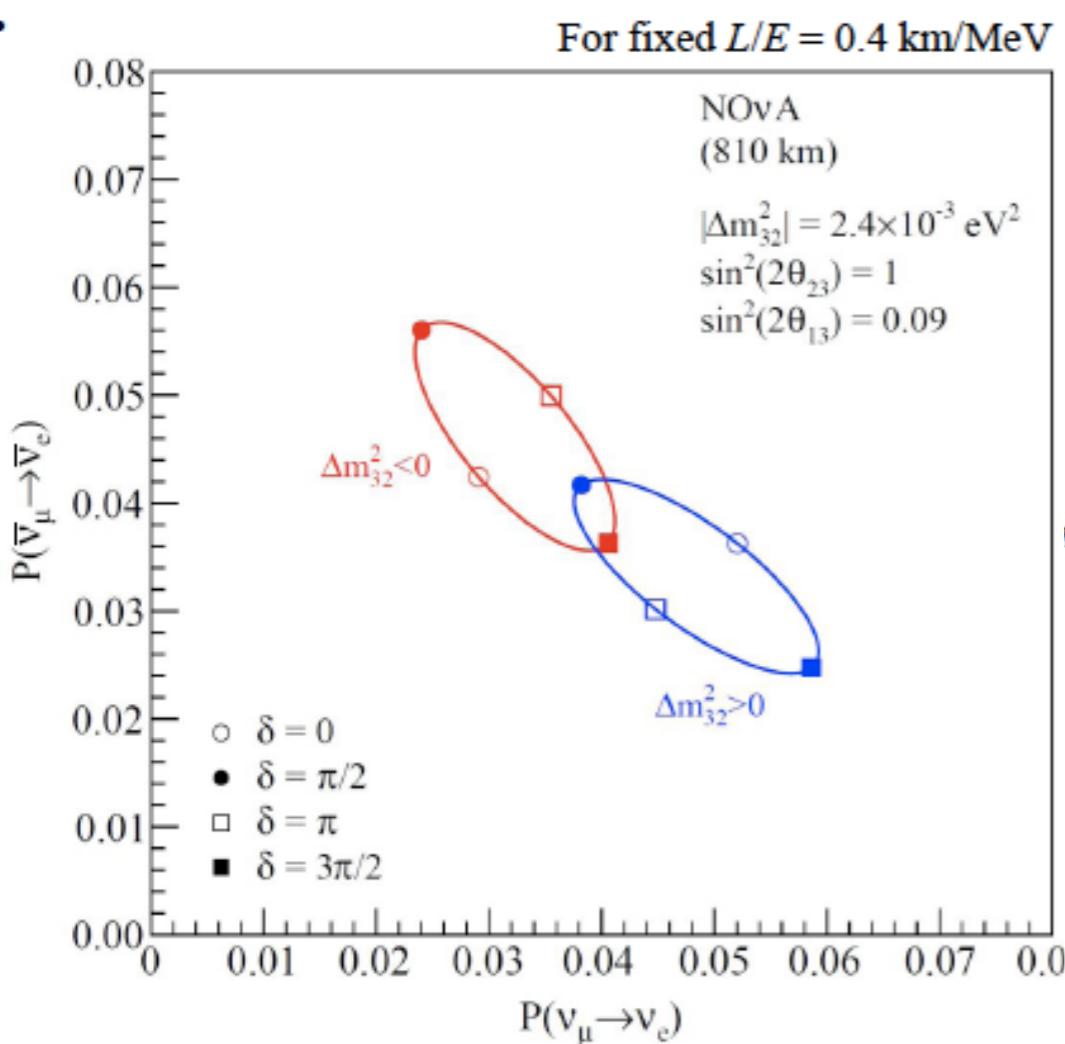


Allowed regions
consistent
with
other experiments

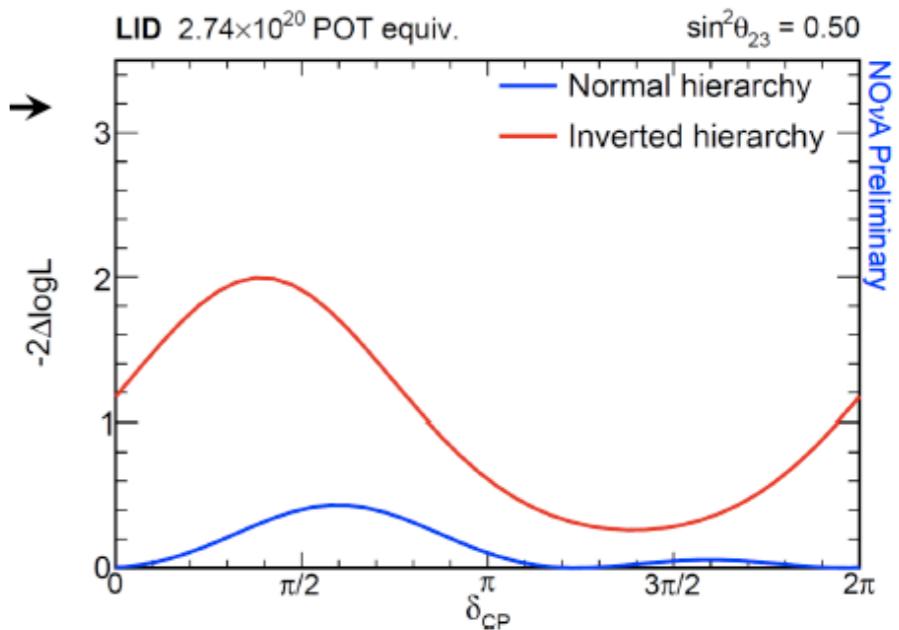
this should not change global results



[R. Patterson, Fermilab JETP Aug. 6, 2015]



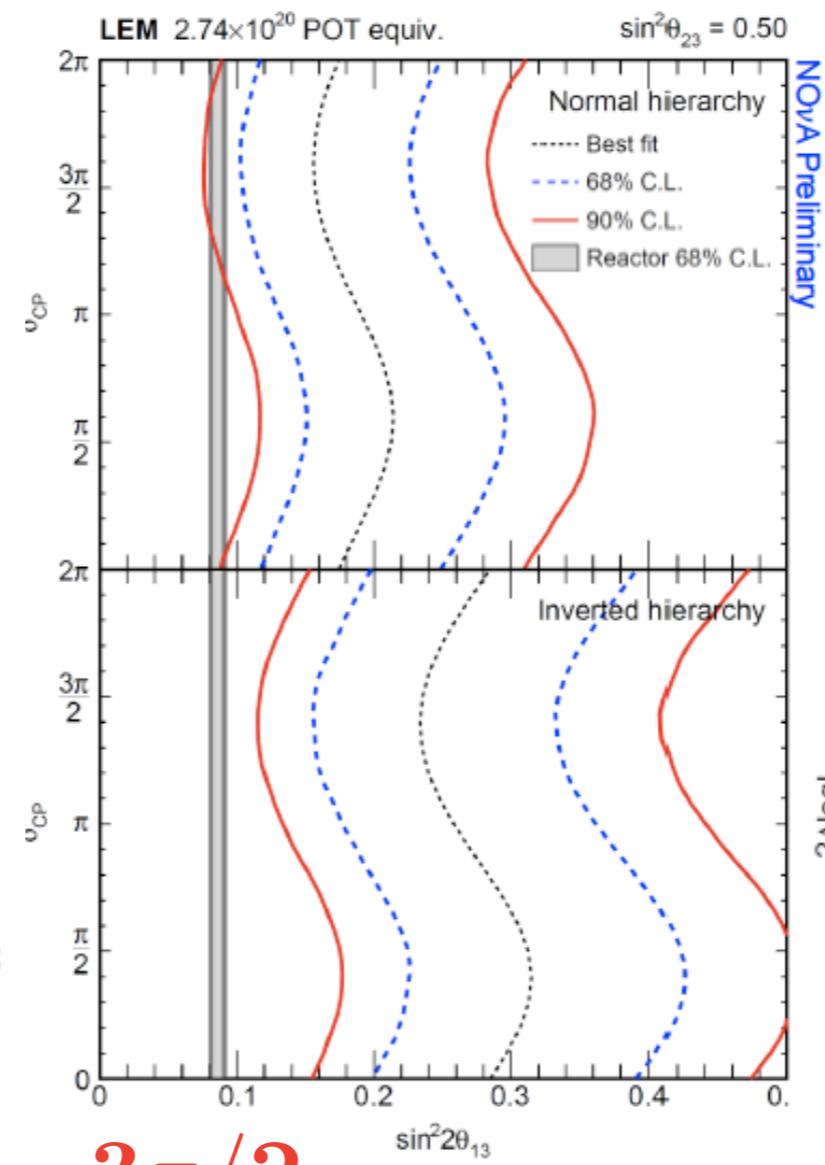
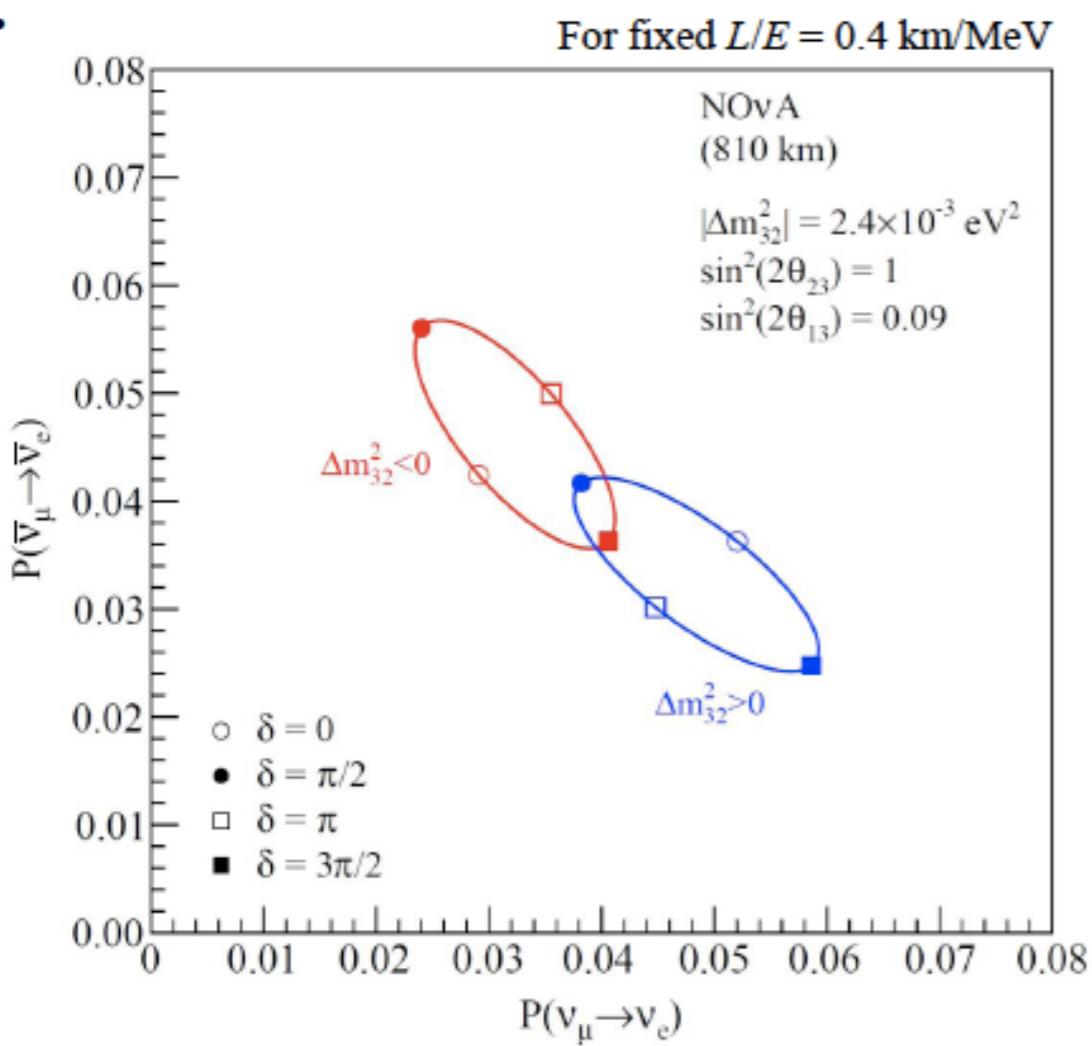
6 events



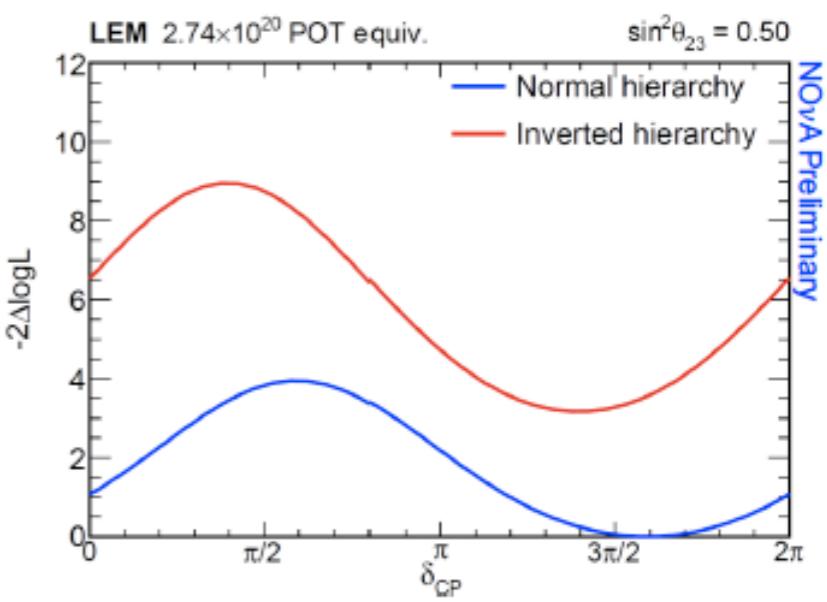
prefer NO & $\delta \sim 3\pi/2$

$\nu_\mu \rightarrow \nu_e$

[R. Patterson, Fermilab JETP Aug. 6, 2015]



II events



prefer NO & $\delta \sim 3\pi/2$



AN AUSPICIOUS FUTURE?



$$\sin^2 \theta_{12} \sim 0.3$$

$$\Delta m_{21}^2 \sim 7.5 \times 10^{-5} \text{ eV}^2$$

$$\sin^2 \theta_{23} \sim 0.5$$

$$|\Delta m_{31,32}^2| \sim 2.5 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 \theta_{13} \sim 0.02$$

all known to better than 5%



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$$\sin^2 \theta_{13} \sim 0.02$$

all known to better than 5%

Undetermined quantities

δ

mass ordering

θ_{23} octant

all data seem to prefer CPV

$$\delta \sim 3\pi/2$$

CODA

$$\sin^2 \theta_{12} \sim 0.3$$

$$\sin^2 \theta_{23} \sim 0.5$$

$$\sin^2 \theta_{13} \sim 0.02$$

$$\Delta m_{21}^2 \sim 7.5 \times 10^{-5} \text{ eV}^2$$

$$|\Delta m_{31,32}^2| \sim 2.5 \times 10^{-3} \text{ eV}^2$$

all known to better than 5%

Undetermined quantities

δ
mass ordering
 θ_{23} octant

NOvA seems to prefer NO
Global Fits prefer IO

But Still not statistically
significant. Stay tuned!



$$\sin^2 \theta_{12} \sim 0.3$$

$$\Delta m_{21}^2 \sim 7.5 \times 10^{-5} \text{ eV}^2$$

$$\sin^2 \theta_{23} \sim 0.5$$

$$|\Delta m_{31,32}^2| \sim 2.5 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 \theta_{13} \sim 0.02$$

all known to better than 5%

Undetermined quantities

δ

mass ordering

θ_{23} octant

Global Fit prefer 2nd
octant slightly for IO

This may change with NOvA

PMNS

NuFIT 2.0 (2014)

$$|U|_{3\sigma} = \begin{pmatrix} 0.801 \rightarrow 0.845 & 0.514 \rightarrow 0.580 & 0.137 \rightarrow 0.158 \\ 0.225 \rightarrow 0.517 & 0.441 \rightarrow 0.699 & 0.614 \rightarrow 0.793 \\ 0.246 \rightarrow 0.529 & 0.464 \rightarrow 0.713 & 0.590 \rightarrow 0.776 \end{pmatrix}$$

CKM

still a long way to go ...

$$|V_{CKM}| = \begin{pmatrix} 0.97425 \pm 0.00022 & 0.2253 \pm 0.0008 & (4.13 \pm 0.49) \times 10^{-3} \\ 0.225 \pm 0.008 & 0.986 \pm 0.016 & (41.1 \pm 1.3) \times 10^{-3} \\ (8.4 \pm 0.6) \times 10^{-3} & (40.0 \pm 2.7) \times 10^{-3} & 1.021 \pm 0.032 \end{pmatrix}$$

Beyond Oscillations: Absolute Mass Observables

Cosmology:

$$\Sigma = m_1 + m_2 + m_3$$

Effective electron neutrino mass:

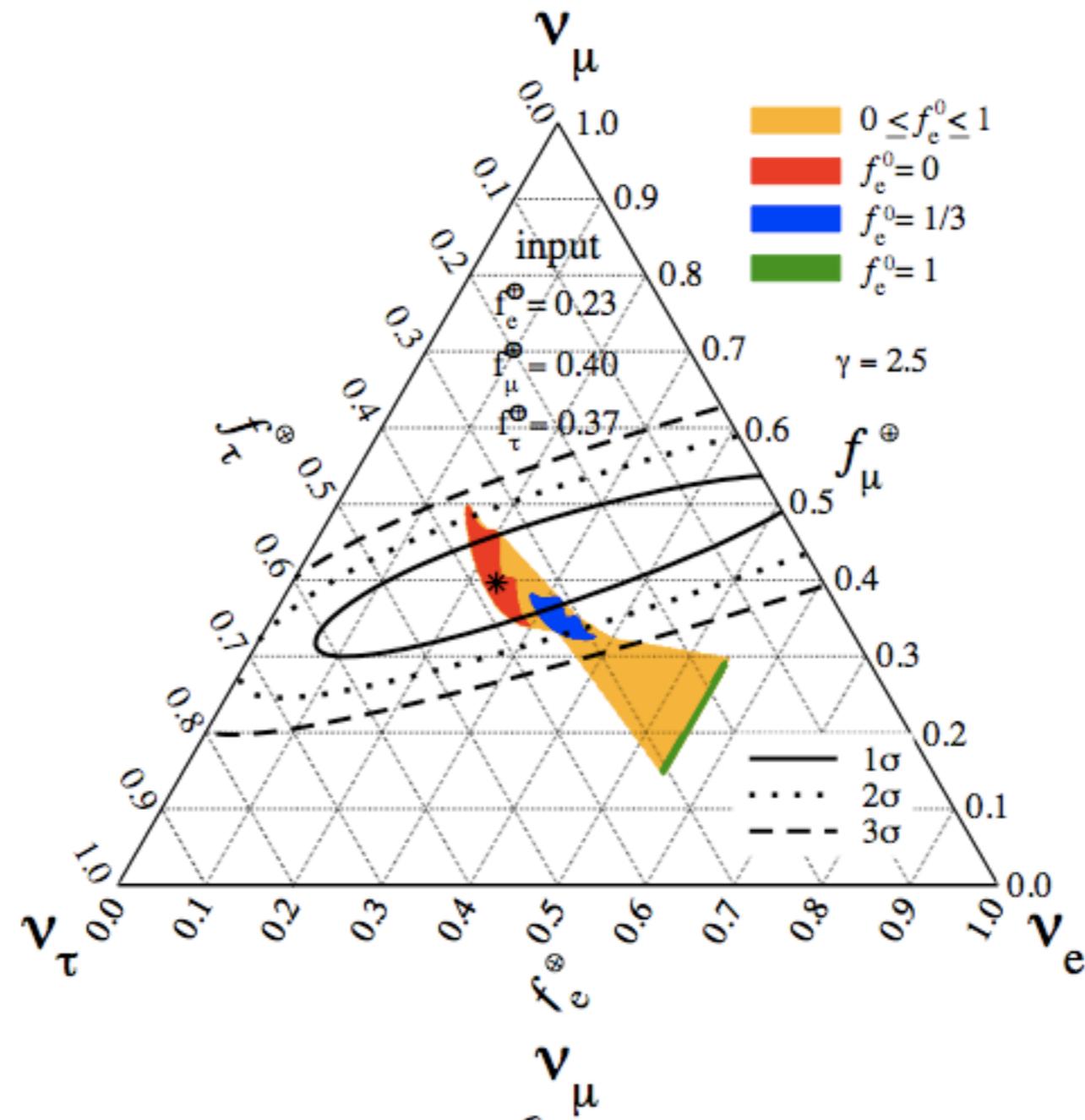
$$m_\beta^2 = [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]$$

Effective Majorana mass:

$$m_{\beta\beta} = |c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\alpha_2} + s_{13}^2 m_3 e^{i\alpha_3}|$$

These observables are correlated by oscillation data

Effect on IceCube Data Interpretation



Keep an open mind for possible new states...
or new subleading effects...

Thank you

